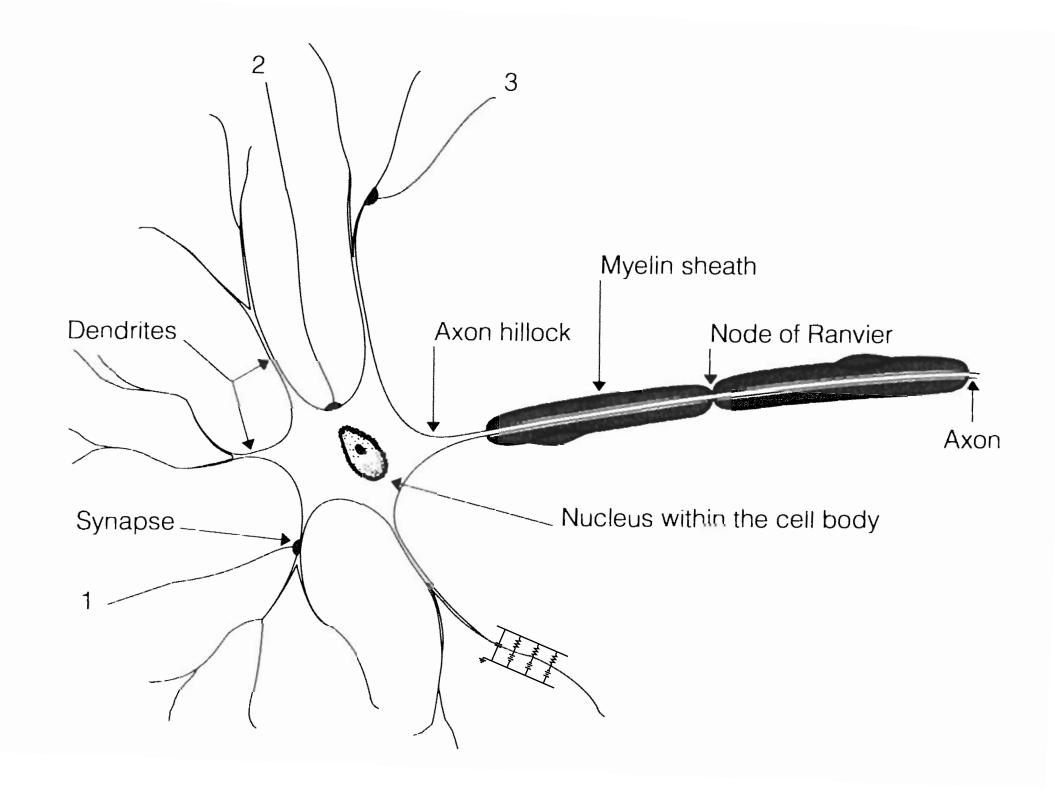
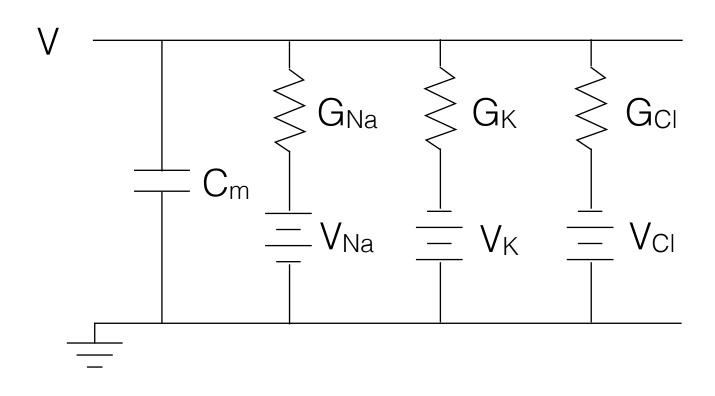
Spiking neurons



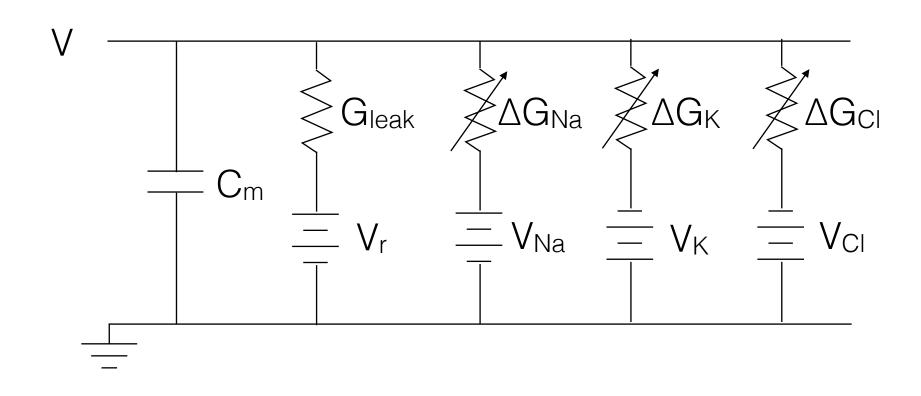
Membrane equation



$$\tau \frac{dV}{dt} + V = \frac{V_{Na} G_{Na} + V_{K} G_{K} + V_{Cl} G_{Cl}}{G_{\text{total}}}$$

$$G_{\text{total}} = G_{Na} + G_K + G_{Cl}$$
 $\tau = \frac{C_m}{G_{\text{total}}}$

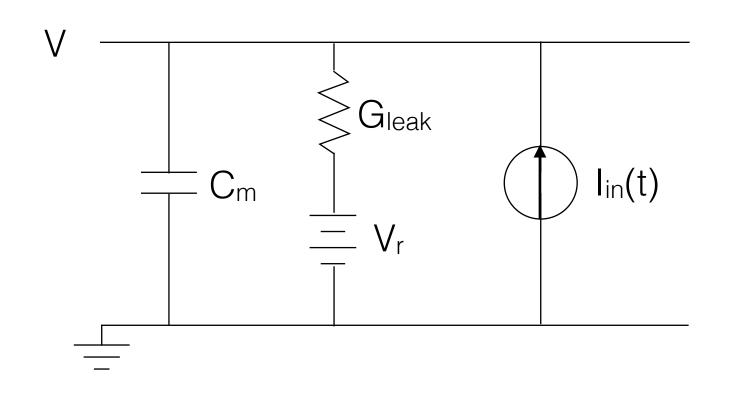
Membrane with synaptic inputs



$$\tau \frac{dV}{dt} + V = \frac{V_r G_{\text{leak}} + V_{Na} \Delta G_{Na} + V_K \Delta G_K + V_{Cl} \Delta G_{Cl}}{G_{\text{total}}}$$

$$G_{\text{total}} = G_{\text{leak}} + \Delta G_{Na} + \Delta G_{K} + \Delta G_{Cl}$$
 $\tau = \frac{C_m}{G_{\text{total}}}$

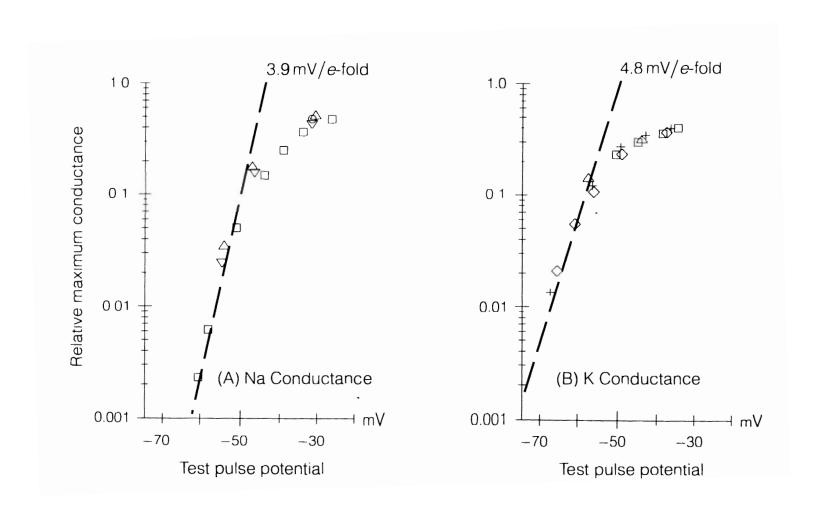
Membrane with input current



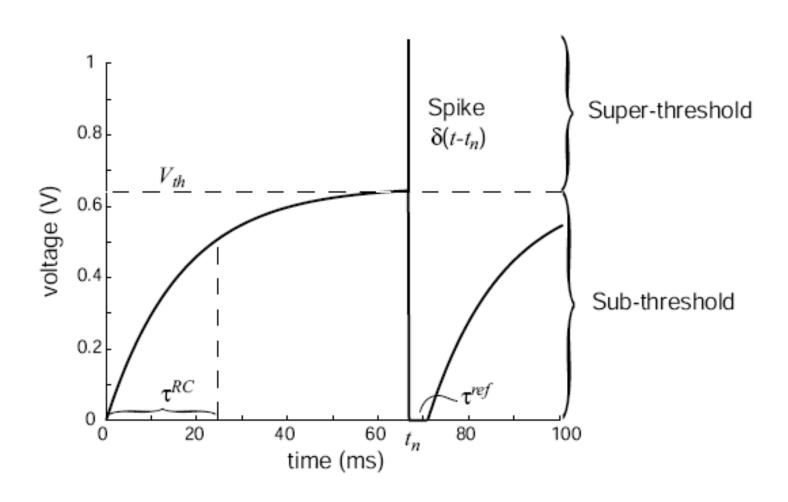
$$\tau \frac{dV}{dt} + V = V_r + \frac{1}{G_{\text{leak}}} I_{\text{in}}(t)$$

$$G_{\text{leak}} = G_{Na} + G_K + G_{Cl}$$
 $au = \frac{C_m}{G_{\text{leak}}}$

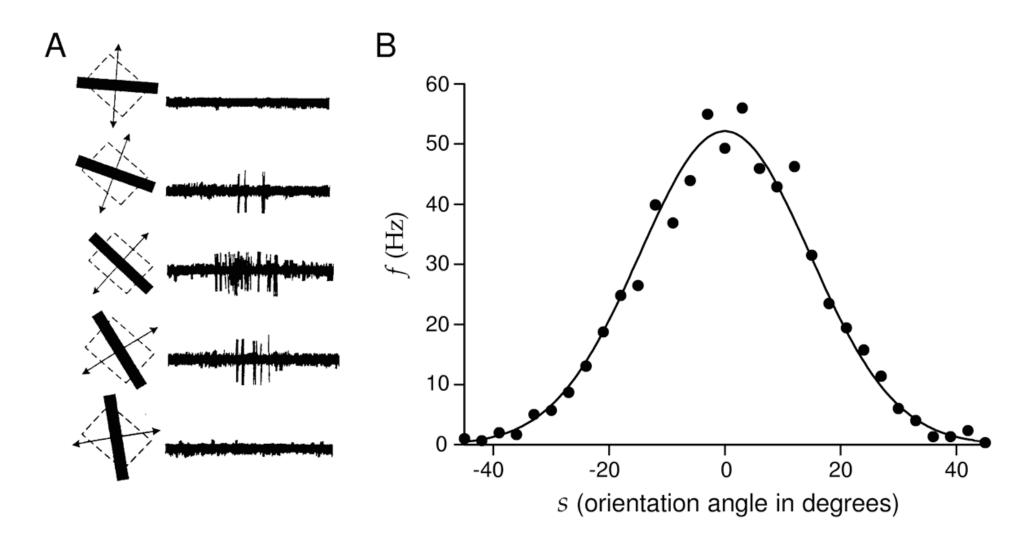
Voltage-gated channels



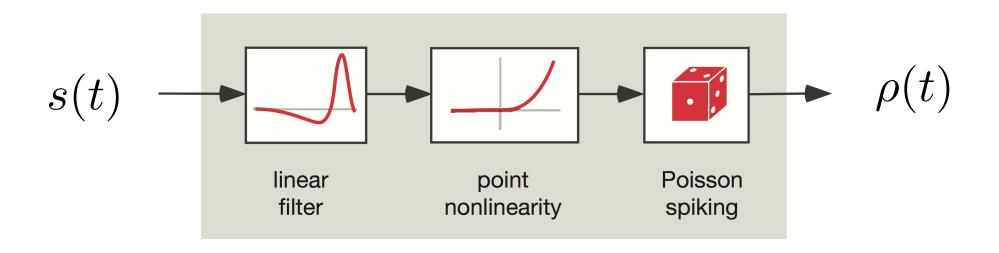
Leaky integrate-and-fire neuron



Rate coding hypothesis: the signal conveyed by a neuron is in the *rate* of spiking. Spiking irregularity is largely due to noise and does not convey information.



Linear - non-linear - Poisson (LNP) model



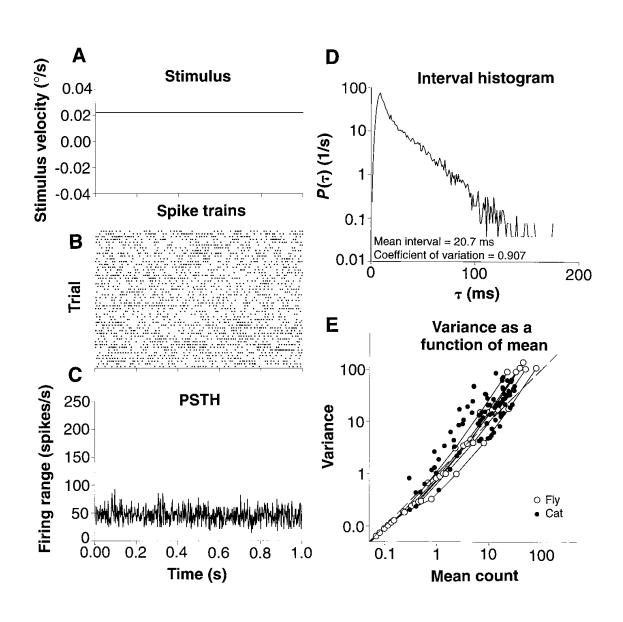
$$P(n) = \frac{\lambda^n e^{-\lambda}}{n!}$$

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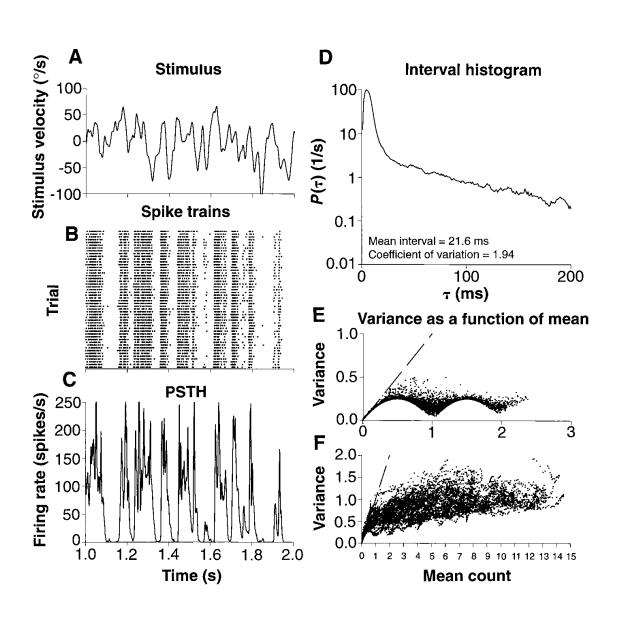
$$P(n) = \frac{\lambda^n e^{-\lambda}}{n!}$$

0.40

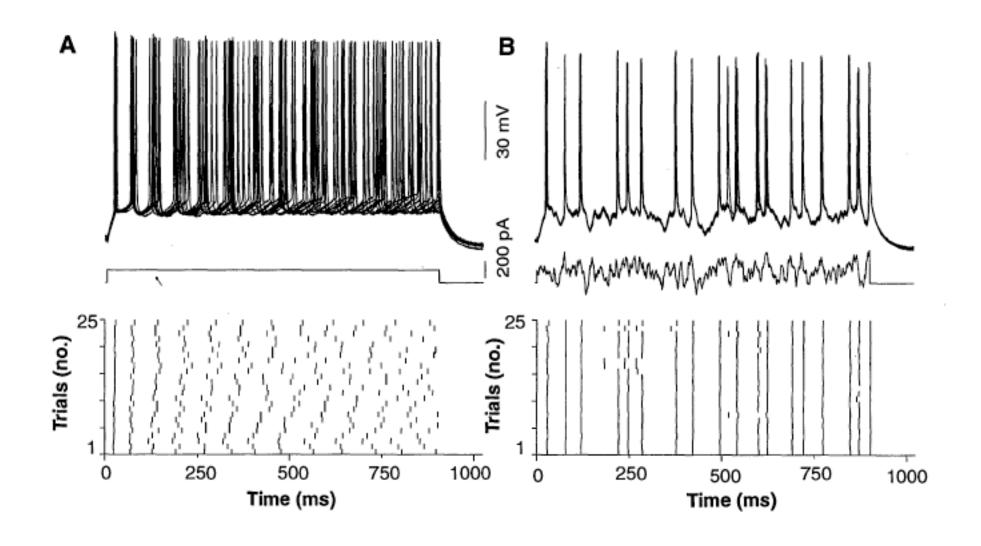
Fly HI neuron - constant stimulus (de Ruyter et al., 1997)



Fly HI neuron - time-varying stimulus (de Ruyter et al., 1997)



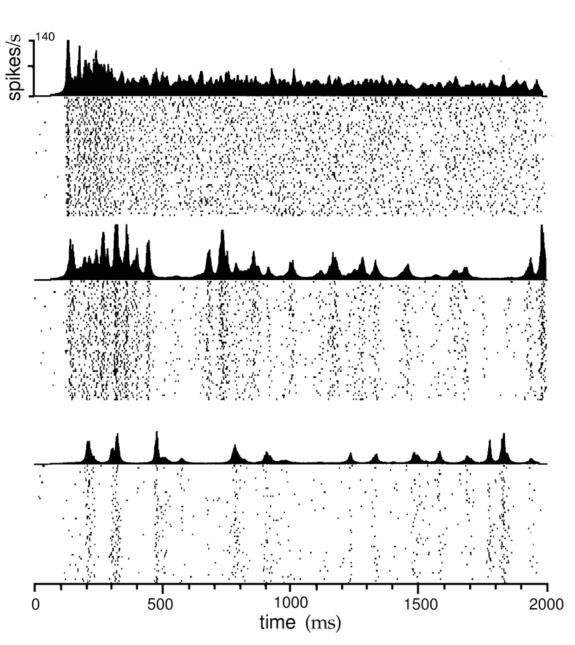
Spike timing can be very precise in response to *time-varying* signals Mainen & Sejnowski (1995)



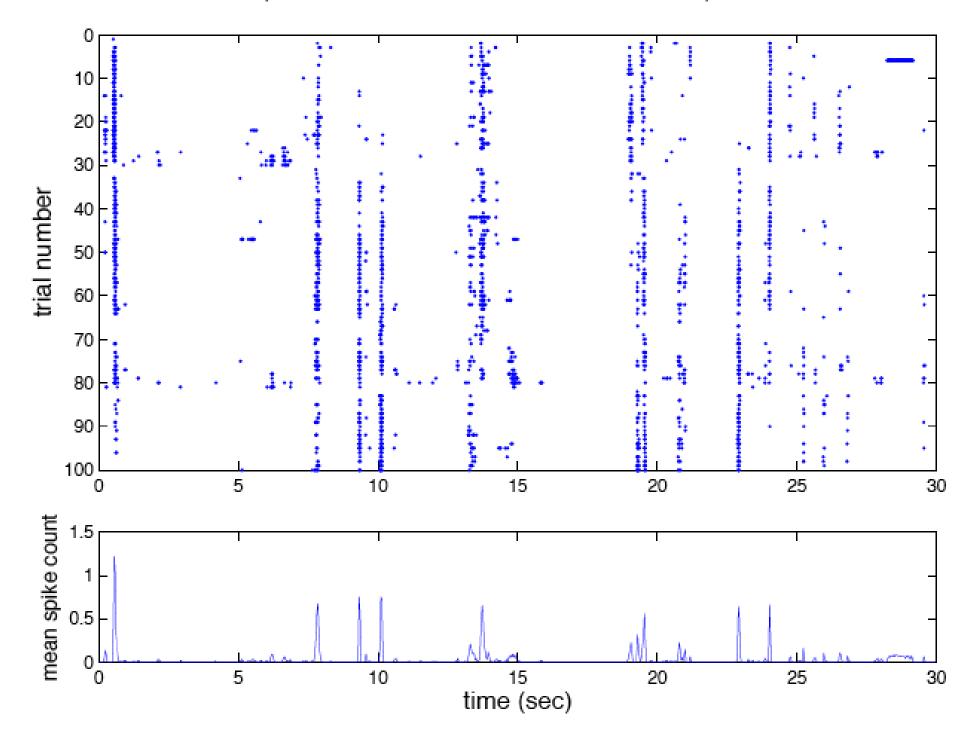
Spike timing can be very precise in response to time-varying signals

MT neuron response to stochastic moving dot stimuli at different levels of coherence (Newsom lab)

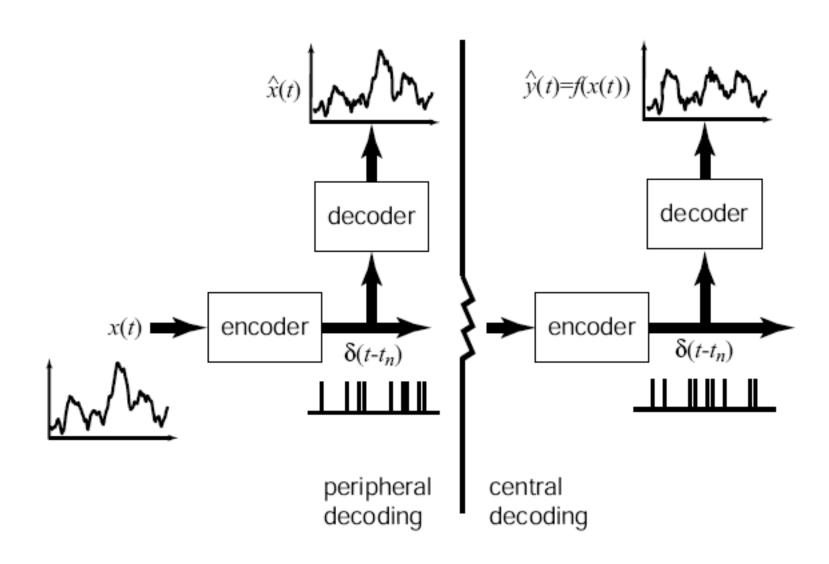
Analysis by Bair & Koch (1996)



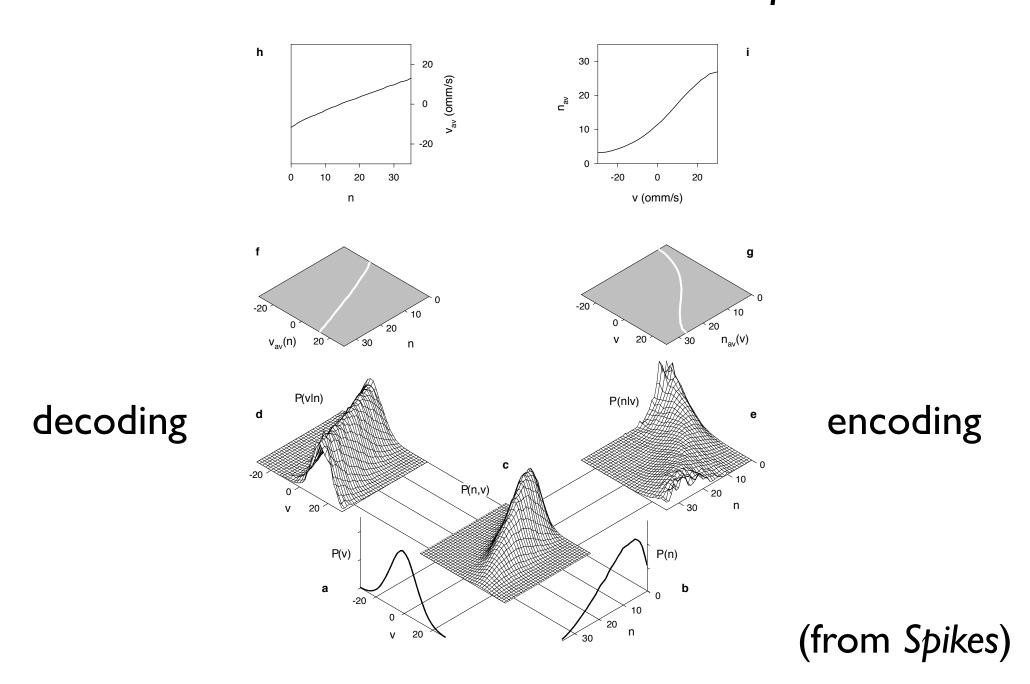
Cat V1 - natural movies (J. Baker, S.C. Yen, C.M. Gray, MSU Bozeman)

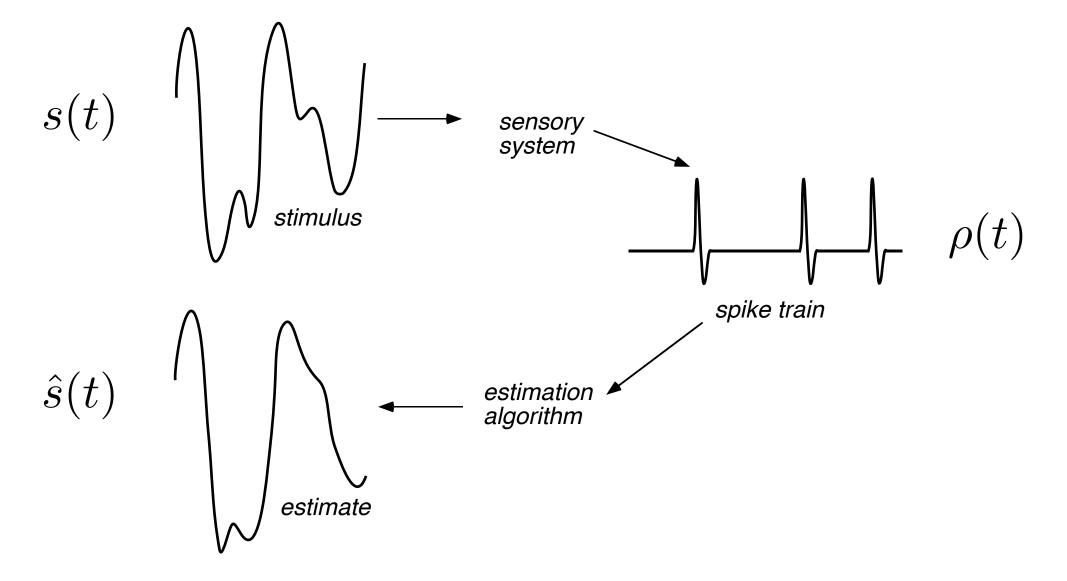


Neural encoding and decoding

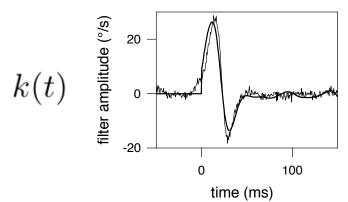


Encoding and decoding are related through the joint distribution over stimulus and response





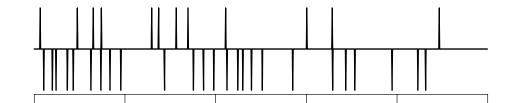
Reconstruction kernel



Fly HI neuron response

$$\rho(t)$$

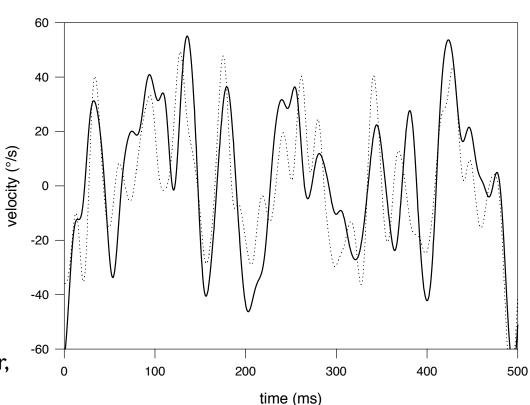
response



Stimulus reconstruction

$$\hat{s}(t) = \rho(t) * k(t)$$

$$\hat{k}(t) = \arg\min_{k(t)} \left\langle \left[s(t) - \rho(t) * k(t) \right]^2 \right\rangle_t$$



From *Spikes*, by Rieke, Warland, de Ruyter, & Bialek

Strategy for estimating information rate

I. Estimate signal from spikes

$$\rho(t) \to \hat{s}(t)$$

2. Compute noise in estimate

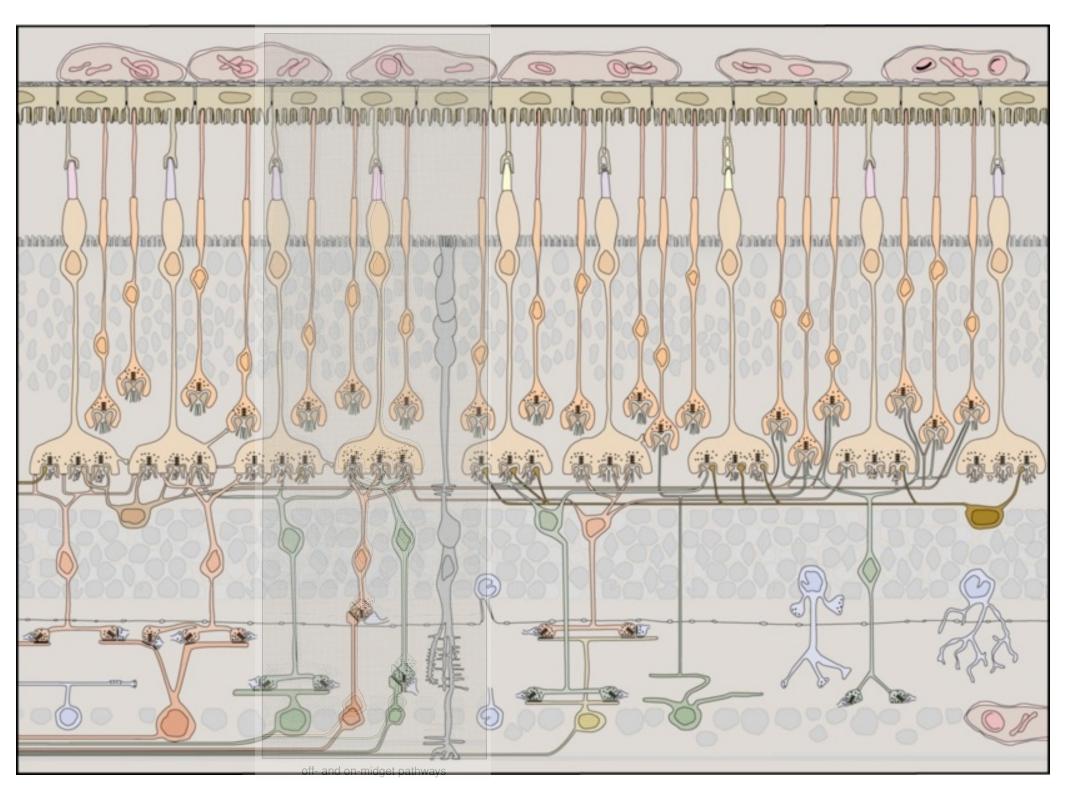
$$\tilde{n}(\omega) = \tilde{s}(\omega) - \hat{\tilde{s}}(\omega)$$

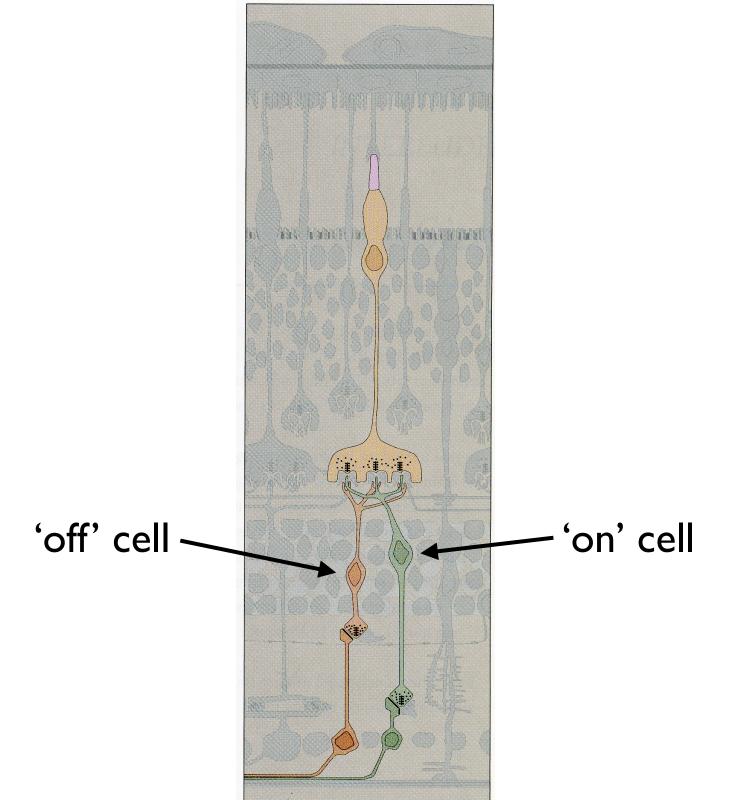
3. Compute SNR

$$SNR(\omega) = \frac{\langle |\tilde{s}(\omega)|^2 \rangle}{\langle |\tilde{n}(\omega)|^2 \rangle}$$

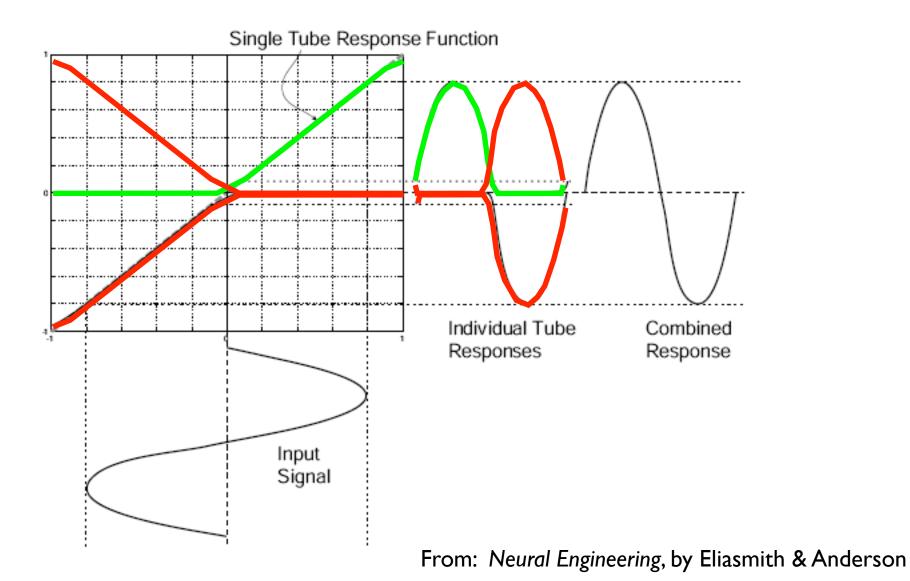
4. Calculate lower bound to information rate from SNR

$$R = \frac{1}{2} \int \frac{d\omega}{2\pi} \log_2[1 + \text{SNR}(\omega)]$$

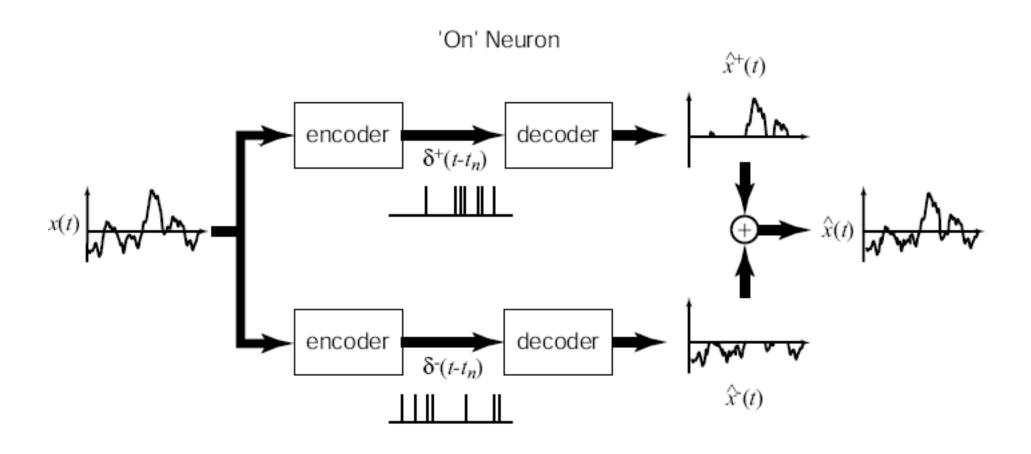




Neural responses are half-wave rectified (action potentials are positive-only). Signals are thus combined in a push-pull fashion, similar to push-pull amplifiers.



Push-Pull decoding



'Off' Neuron

Efficient coding model of retina

(Karklin & Simoncelli 2012)

