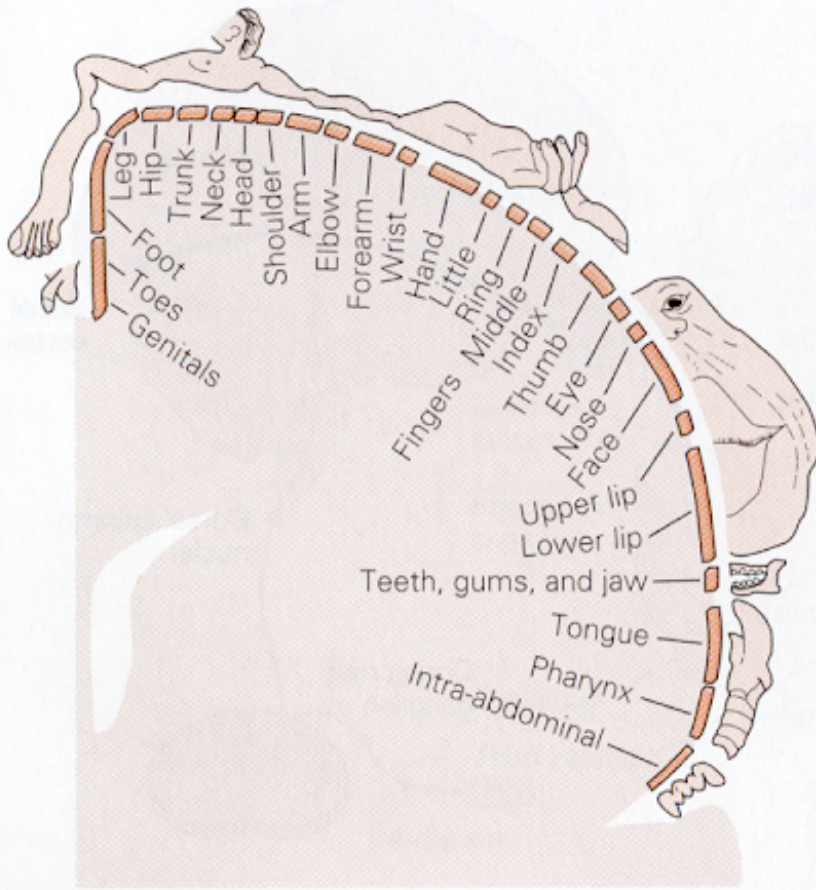


Self-organizing maps

Cortical maps

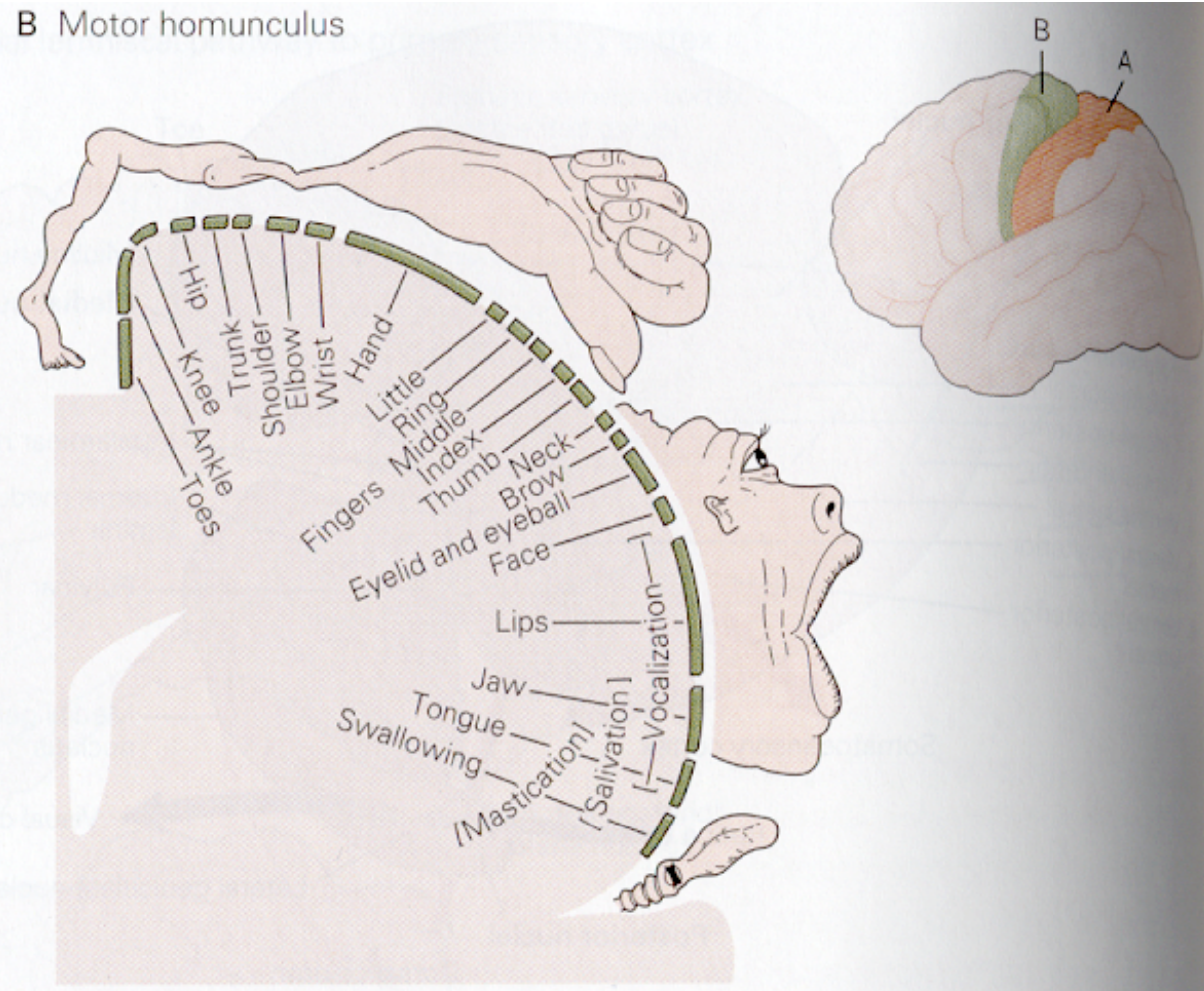
A Sensory homunculus



Medial

Lateral

B Motor homunculus

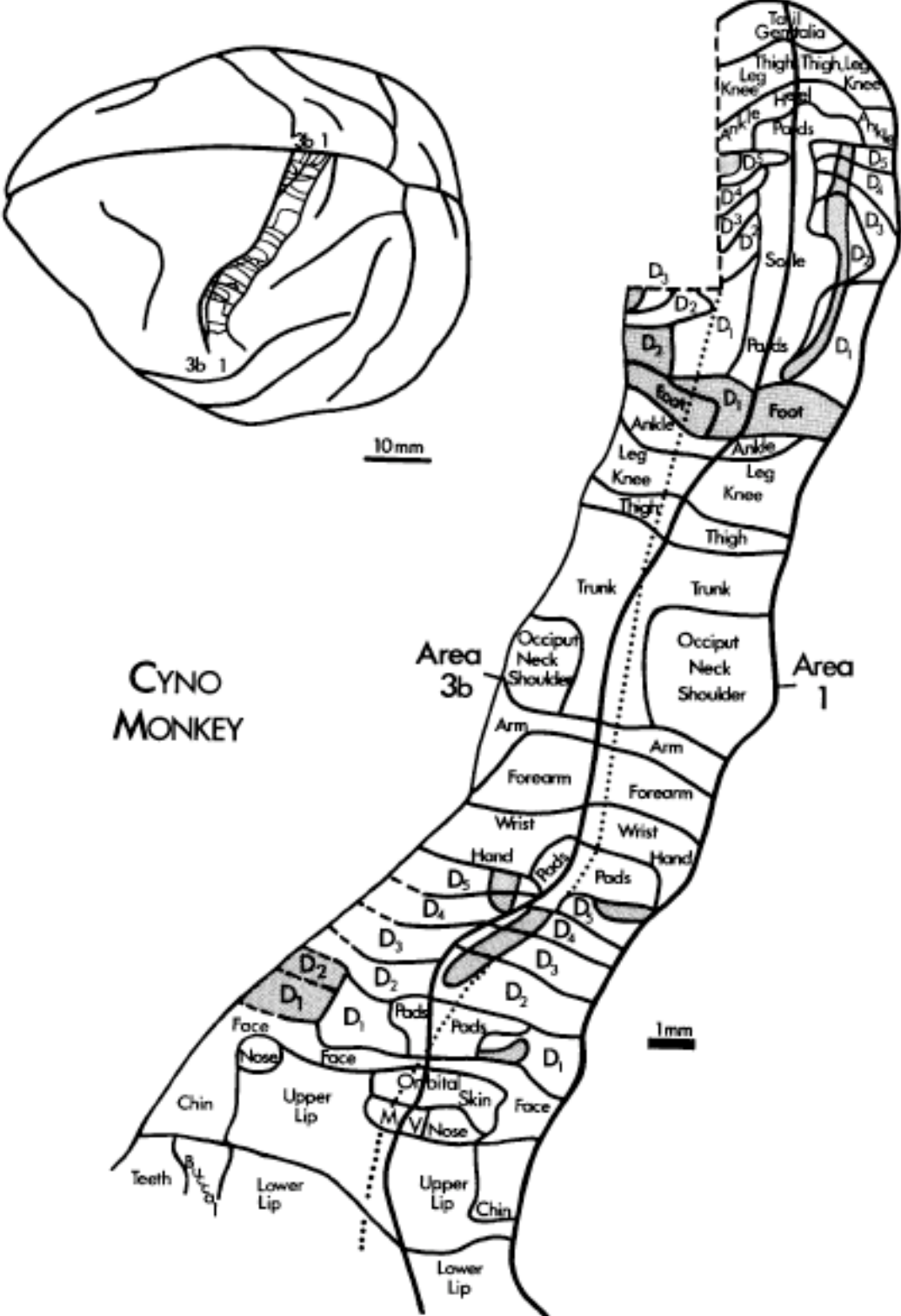


Medial

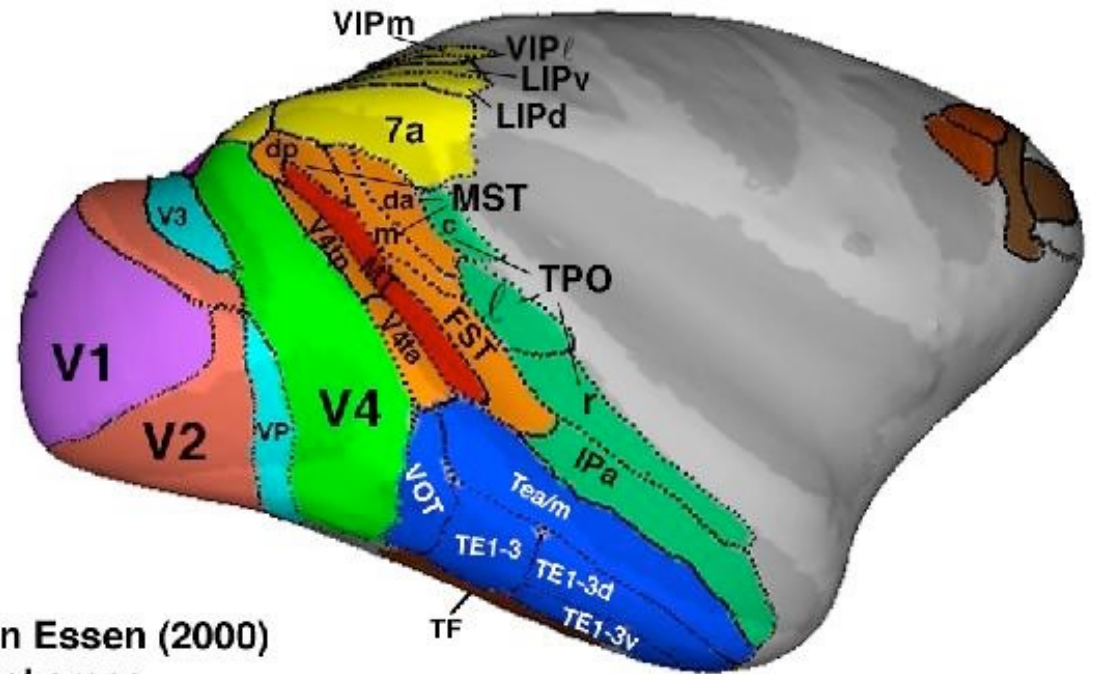
Lateral

(from Penfield & Rasmussen, 1950)

Somatosensory cortex

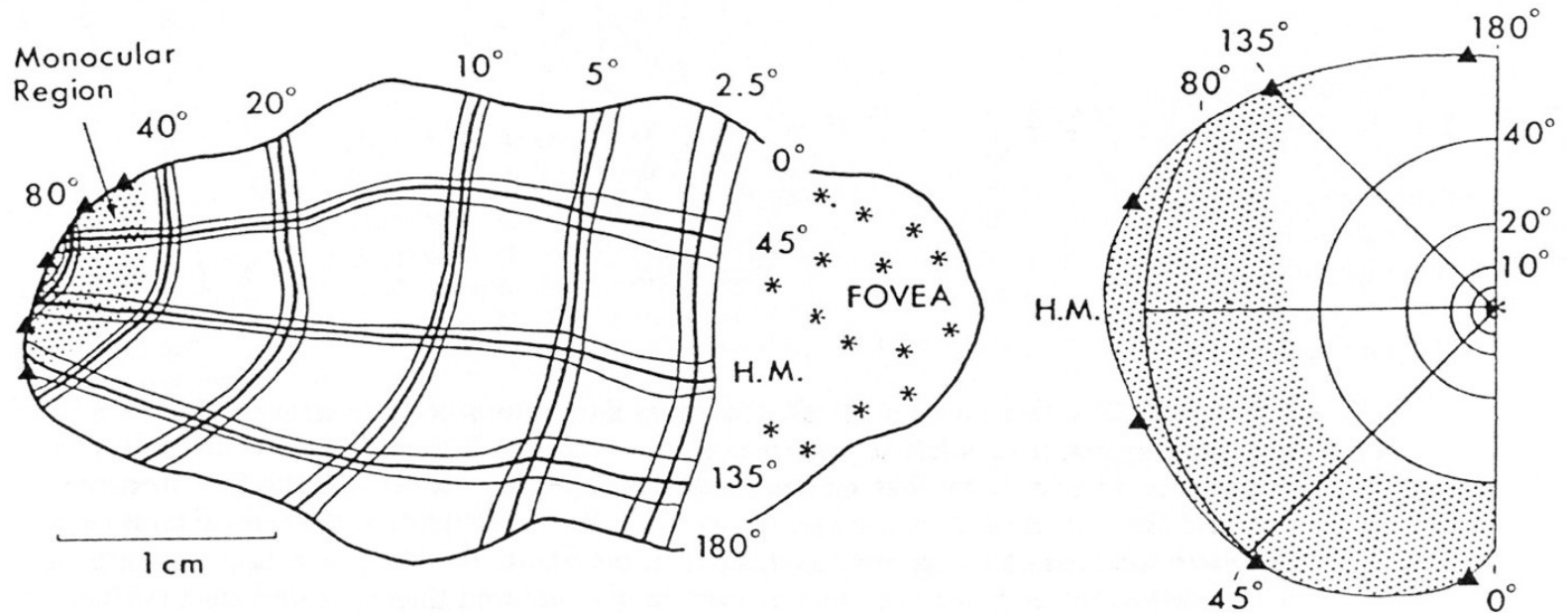


Visual cortex

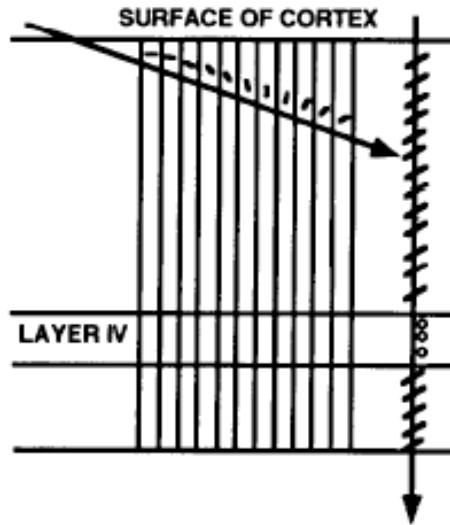


Lewis & Van Essen (2000)
Visual areas

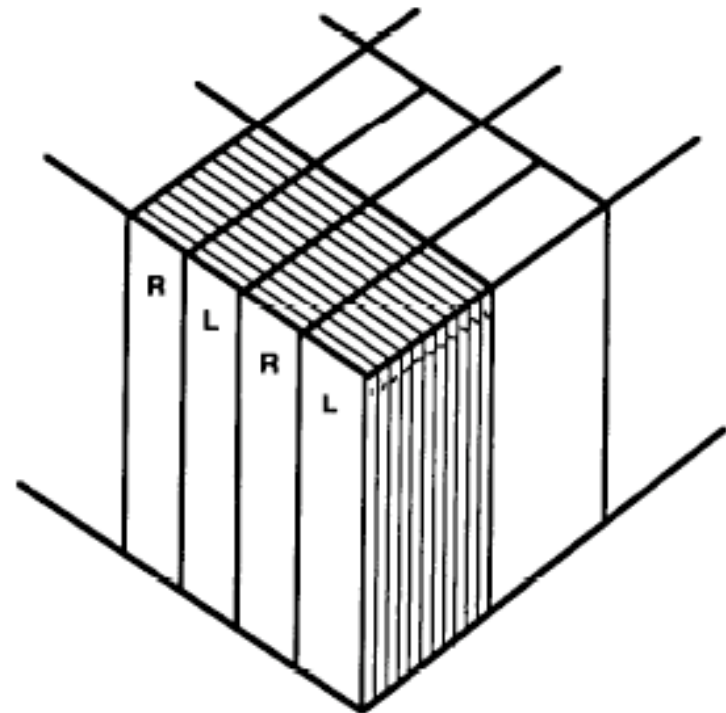
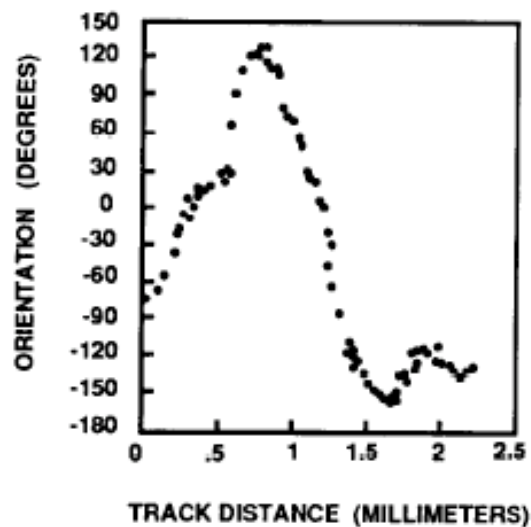
VI topographic map



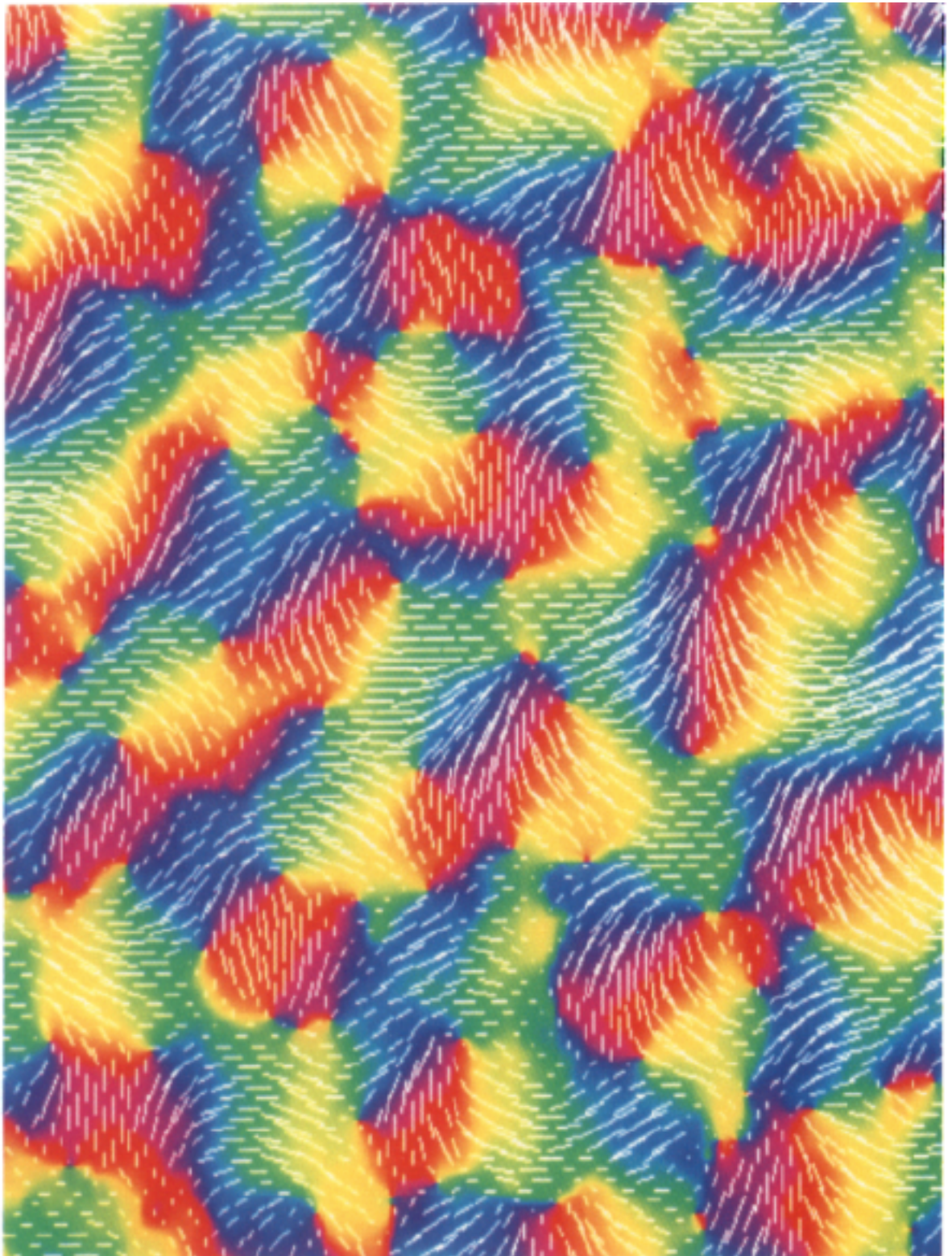
Orientation selectivity changes in a regular manner across the surface of VI



Hubel & Wiesel's
“ice cube tray model”

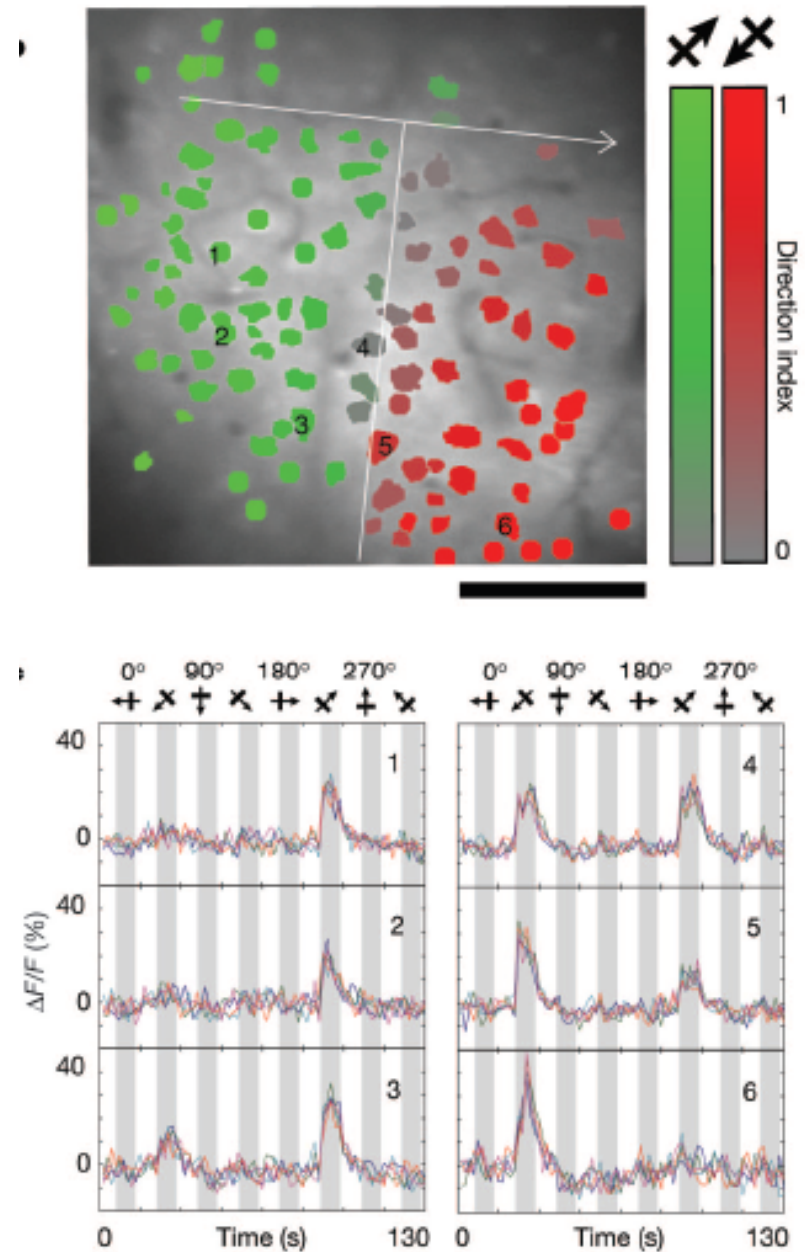
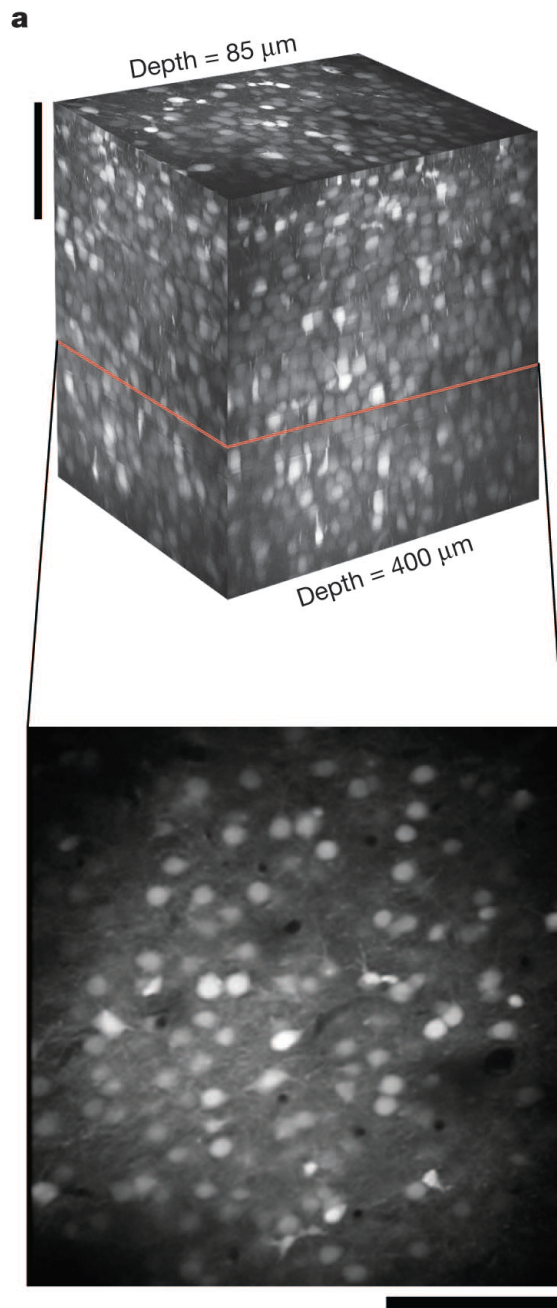


Orientation
maps in V1
(Blasdel 1992)



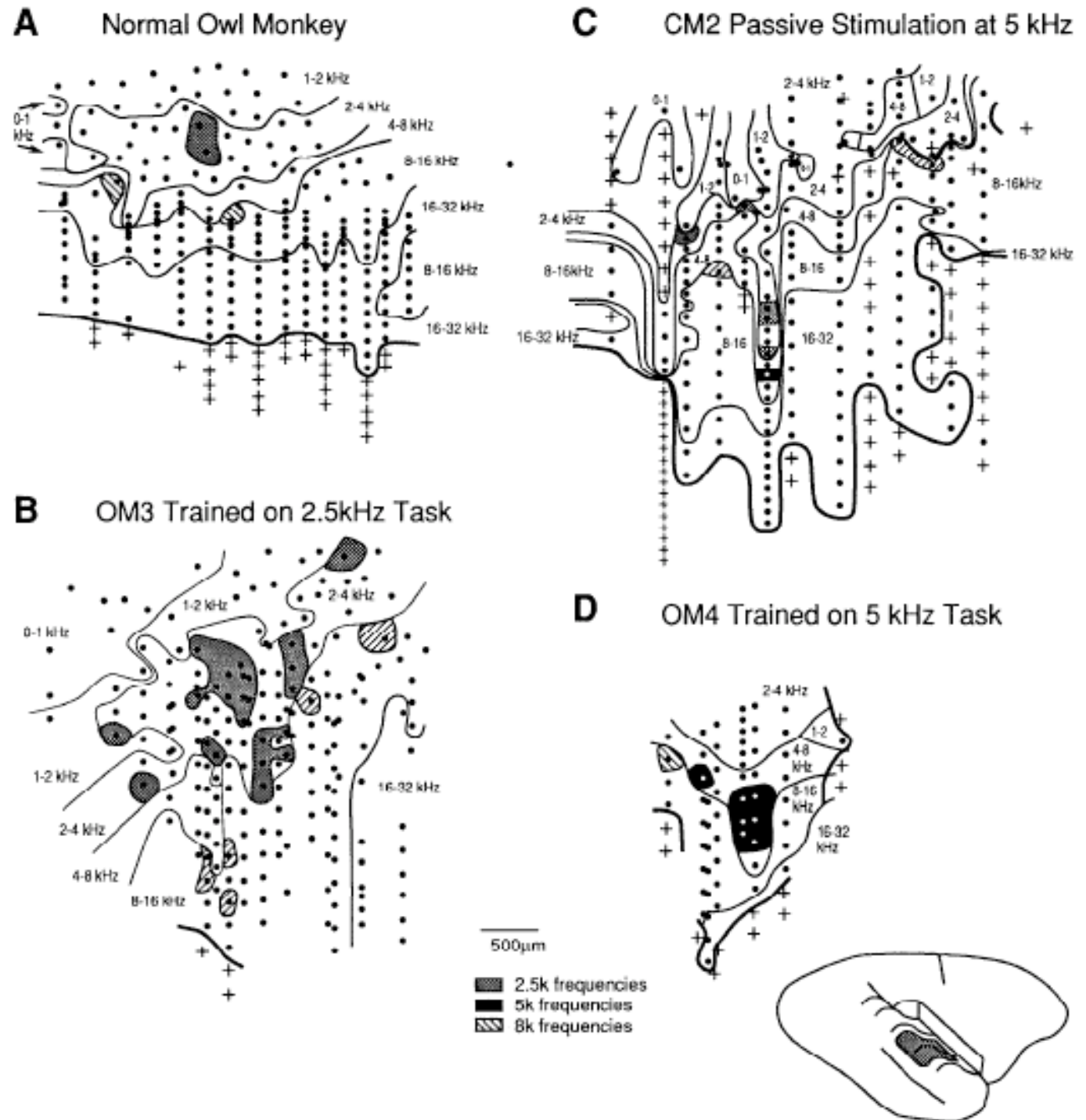
Direction selective cells in cat area 18

(Ca⁺⁺ imaging - Ohki, Chung, Ch'ng, Kara, Reid, 2005)

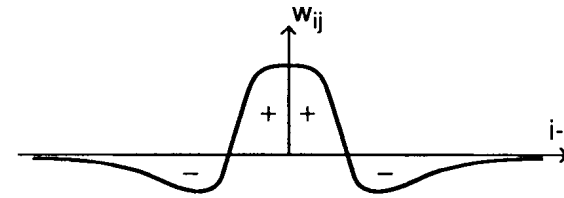


Cortical maps are Plastic

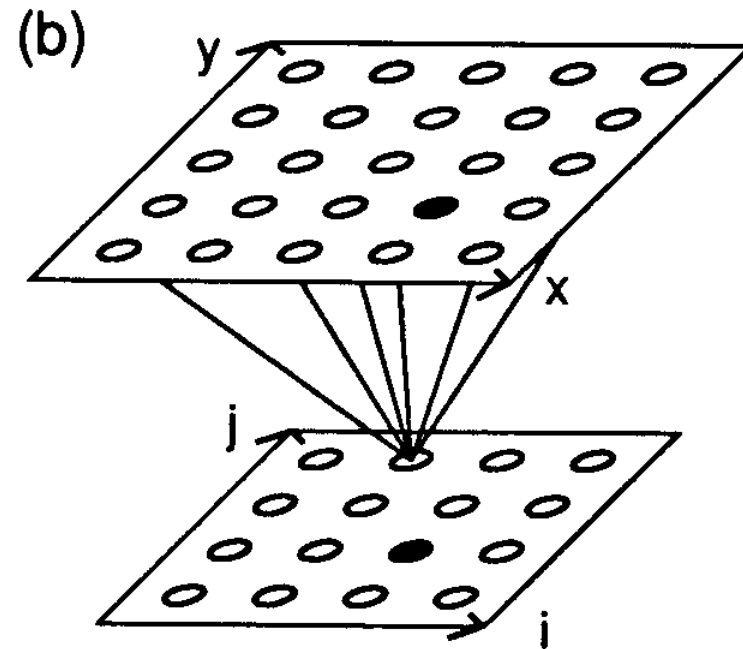
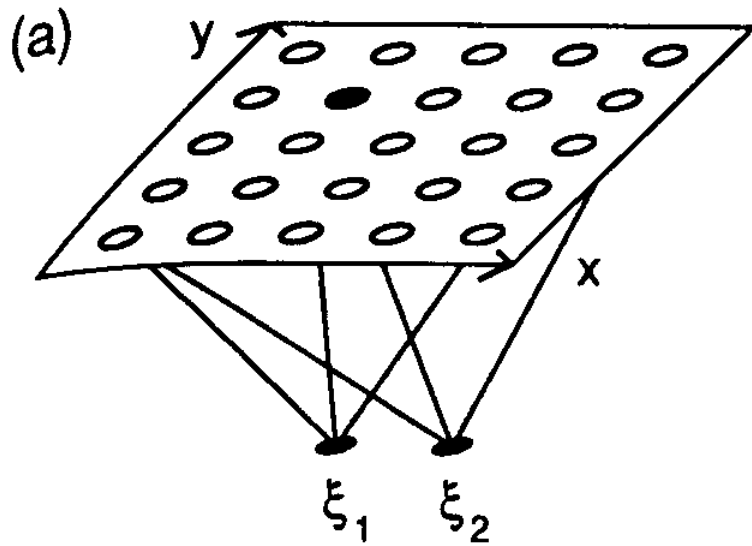
(monkey auditory cortex - Recanzone, Schreiner & Merzenich, 1993)



Self-organizing maps



horizontal connections



output

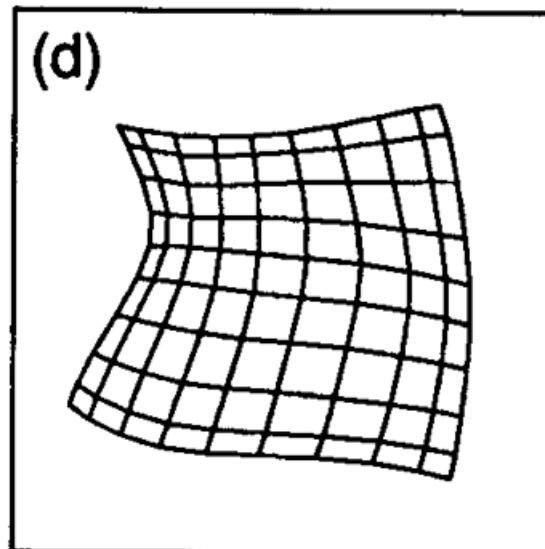
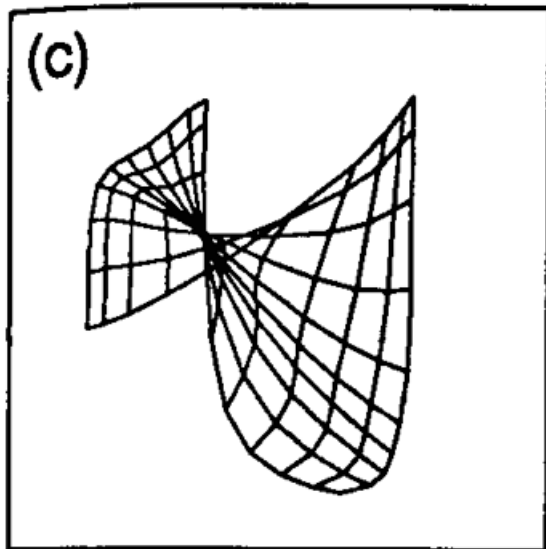
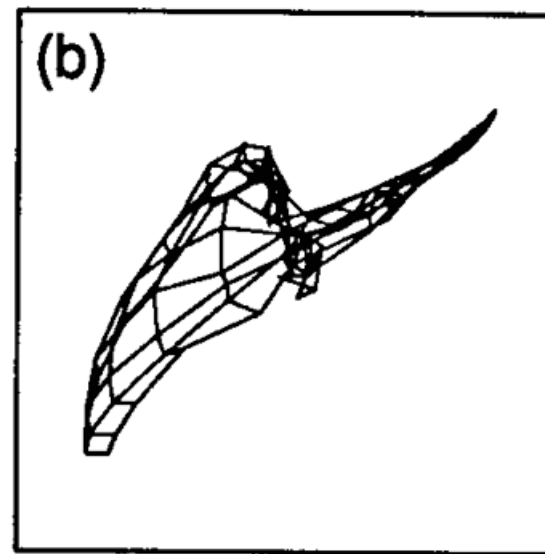
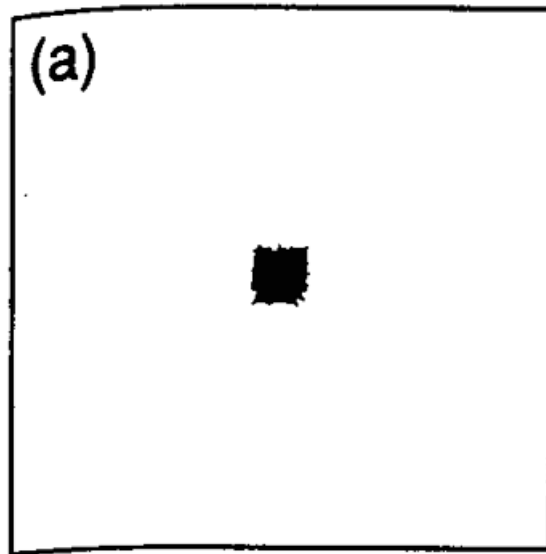
input

Kohonen's algorithm

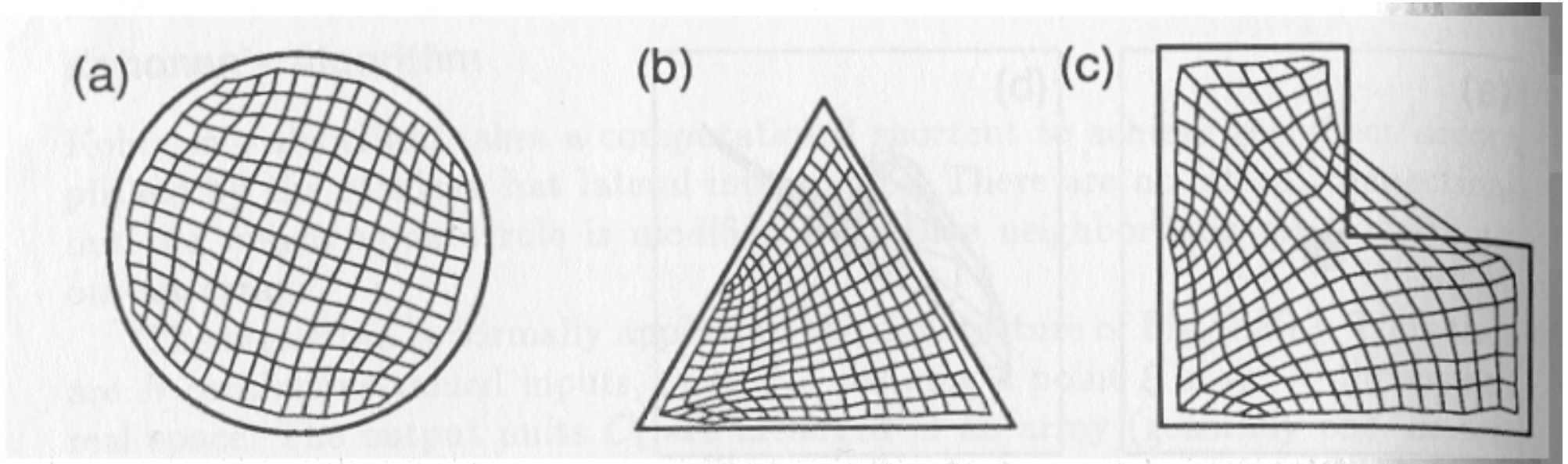
$$\Delta \mathbf{w}_i = \eta \Lambda(i, i^*) (\mathbf{x} - \mathbf{w}_i)$$

$$\Lambda(i, i^*) = e^{-\frac{|\mathbf{r}_i - \mathbf{r}_{i^*}|^2}{2\sigma^2}}$$

Kohonen's algorithm applied to a 2D input array



Map conforms to topology of input data



Kohonen's algorithm

Energy function:

$$\begin{aligned} E(\{\mathbf{w}_i\}) &= \frac{1}{2} \sum_{i,k,\mu} M_k^\mu \Lambda(i, k) |\mathbf{x}^{(\mu)} - \mathbf{w}_i|^2 \\ &= \frac{1}{2} \sum_{i,\mu} \Lambda(i, i^*) |\mathbf{x}^{(\mu)} - \mathbf{w}_i|^2 \end{aligned}$$

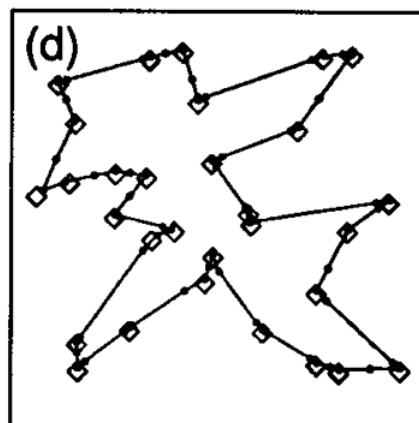
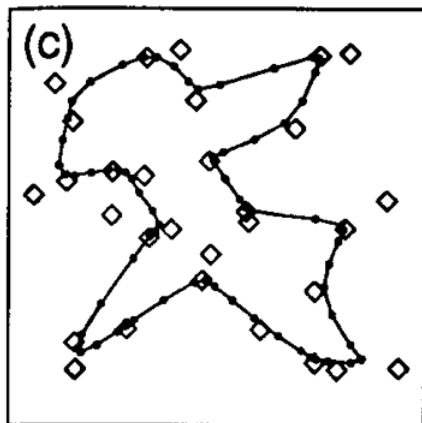
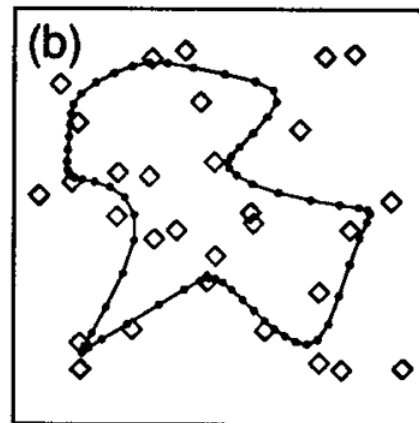
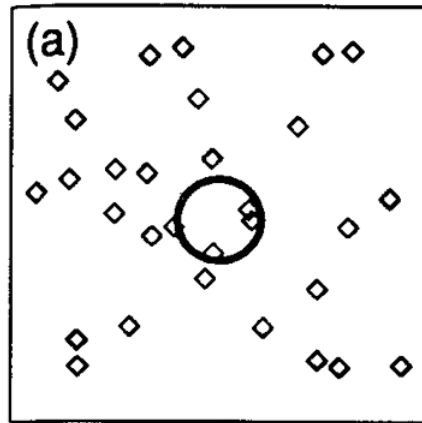
Gradient descent:

$$\begin{aligned} \Delta \mathbf{w}_i &= -\eta \frac{\partial E}{\partial \mathbf{w}_i} \\ &= \eta \sum_{\mu} \Lambda(i, i^*) (\mathbf{x}^{(\mu)} - \mathbf{w}_i) \end{aligned}$$

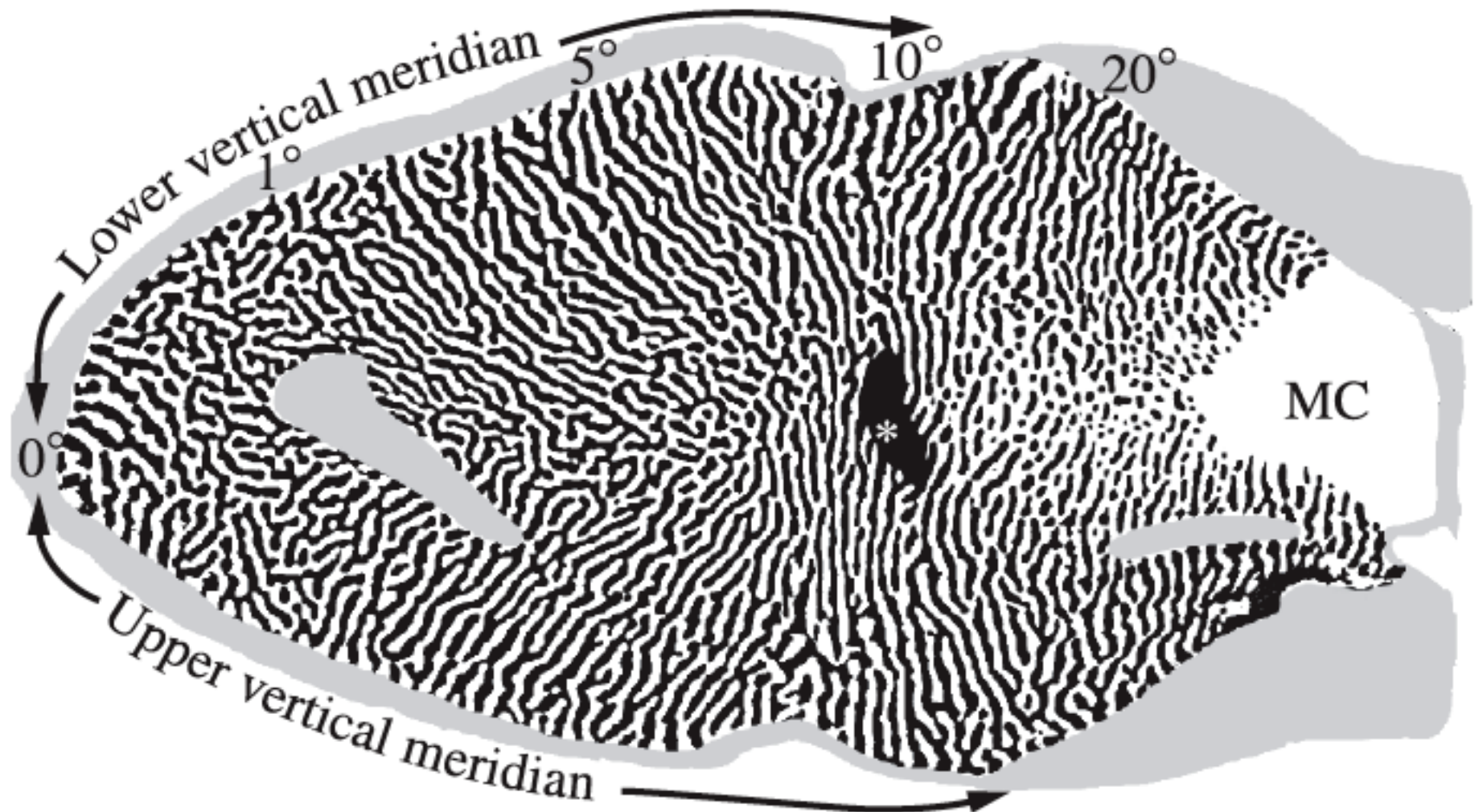
Traveling salesman problem (‘Elastic net’ - Durbin & Willshaw 1987)

$$\Delta \mathbf{w}_i = \eta \left(\sum_{\mu} \Lambda^{\mu}(i) (\xi^{\mu} - \mathbf{w}_i) + \kappa(\mathbf{w}_{i+1} - 2\mathbf{w}_i + \mathbf{w}_{i-1}) \right) \quad \Lambda^{\mu}(i) = \frac{\exp(-|\xi^{\mu} - \mathbf{w}_i|^2/2\sigma^2)}{\sum_j \exp(-|\xi^{\mu} - \mathbf{w}_j|^2/2\sigma^2)}$$

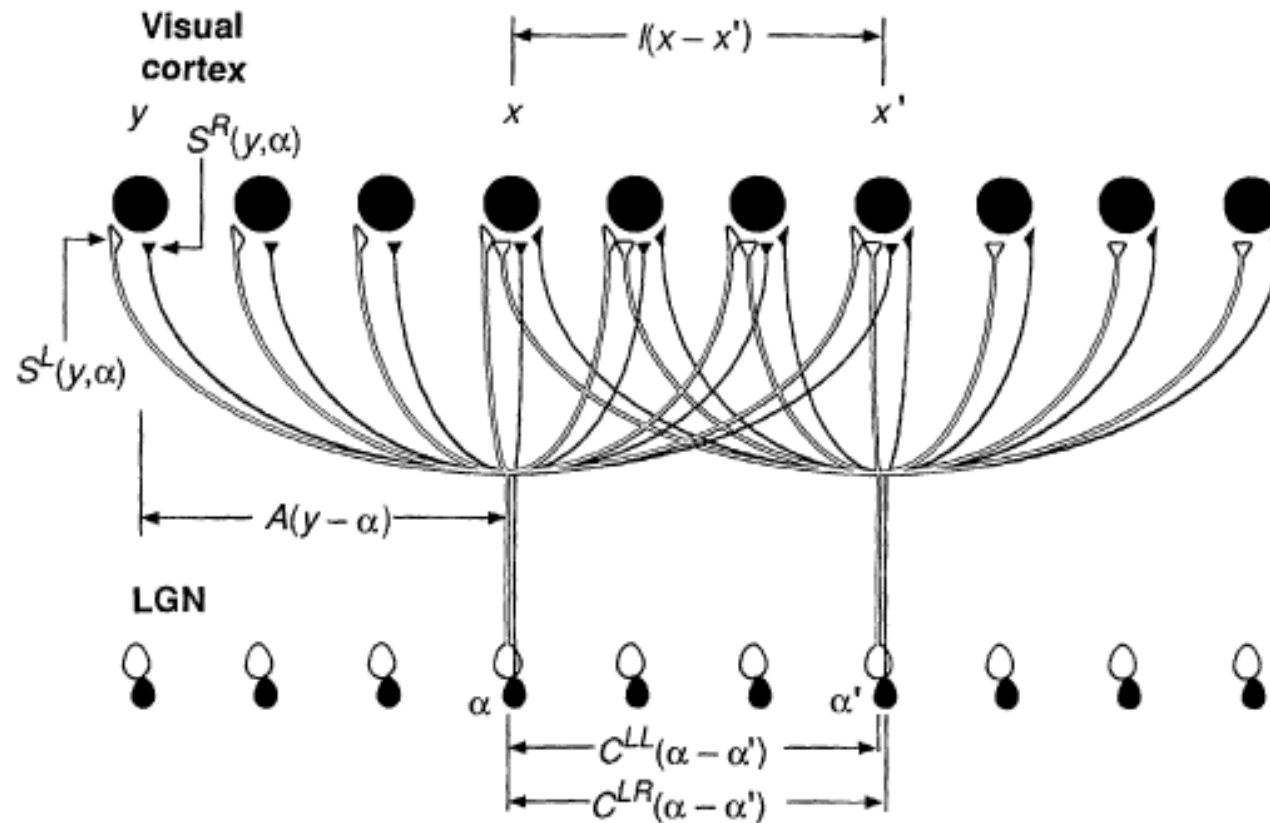
$$E\{\mathbf{w}_i\} = -\sigma \sum_{\mu} \log \left[\sum_i \exp(-|\xi^{\mu} - \mathbf{w}_i|^2/2\sigma^2) \right] + \frac{\kappa}{2} \sum_i |\mathbf{w}_{i+1} - \mathbf{w}_i|^2$$



Ocular dominance columns (Horton)

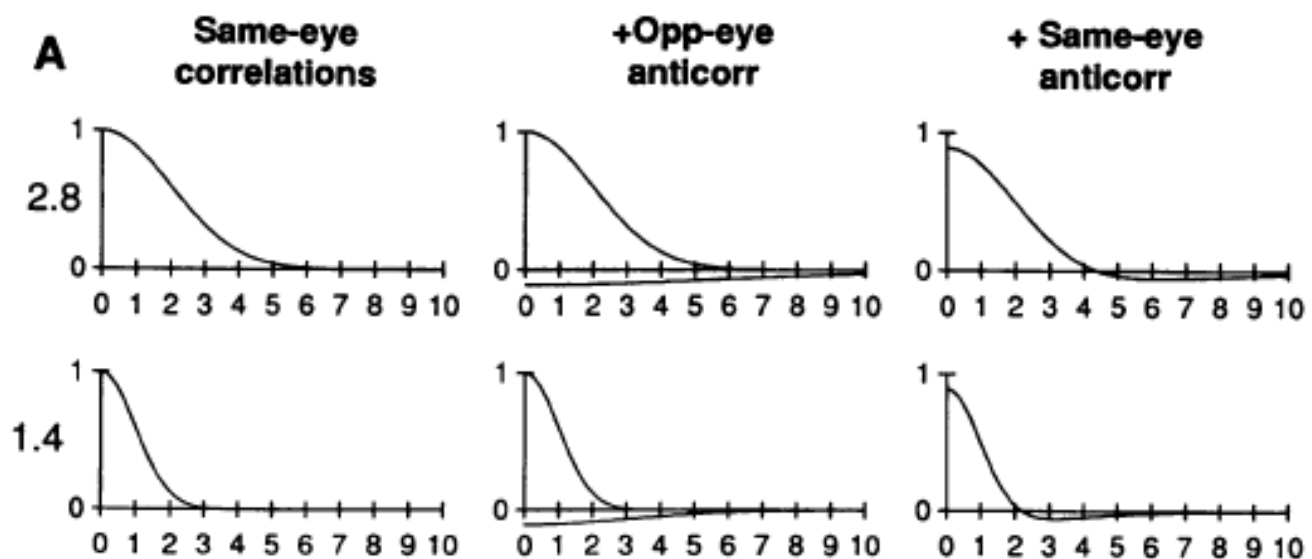


Model of ocular dominance column development (Miller, Keller & Stryker, 1989)

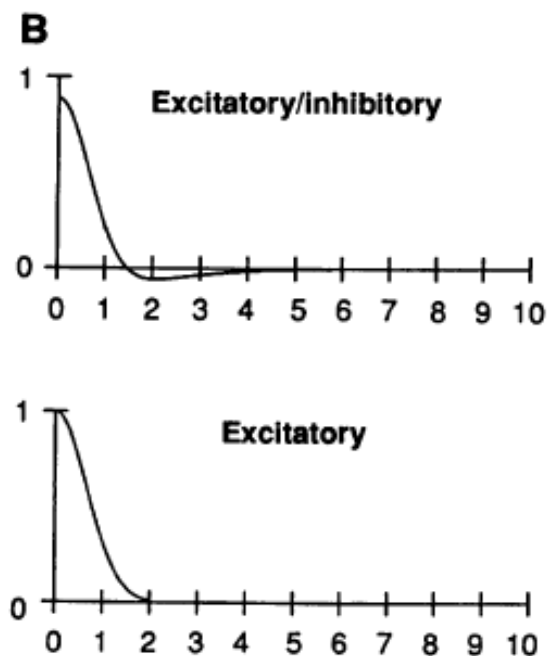


$$\frac{dS^L(x, \alpha, t)}{dt} = \lambda A(x - \alpha) \sum_{y, \beta} I(x - y) [C^{LL}(\alpha - \beta) S^L(y, \beta, t) + C^{LR}(\alpha - \beta) S^R(y, \beta, t)] - \gamma S^L(x, \alpha, t) - \varepsilon A(x - \alpha)$$

$$C(\alpha - \beta)$$

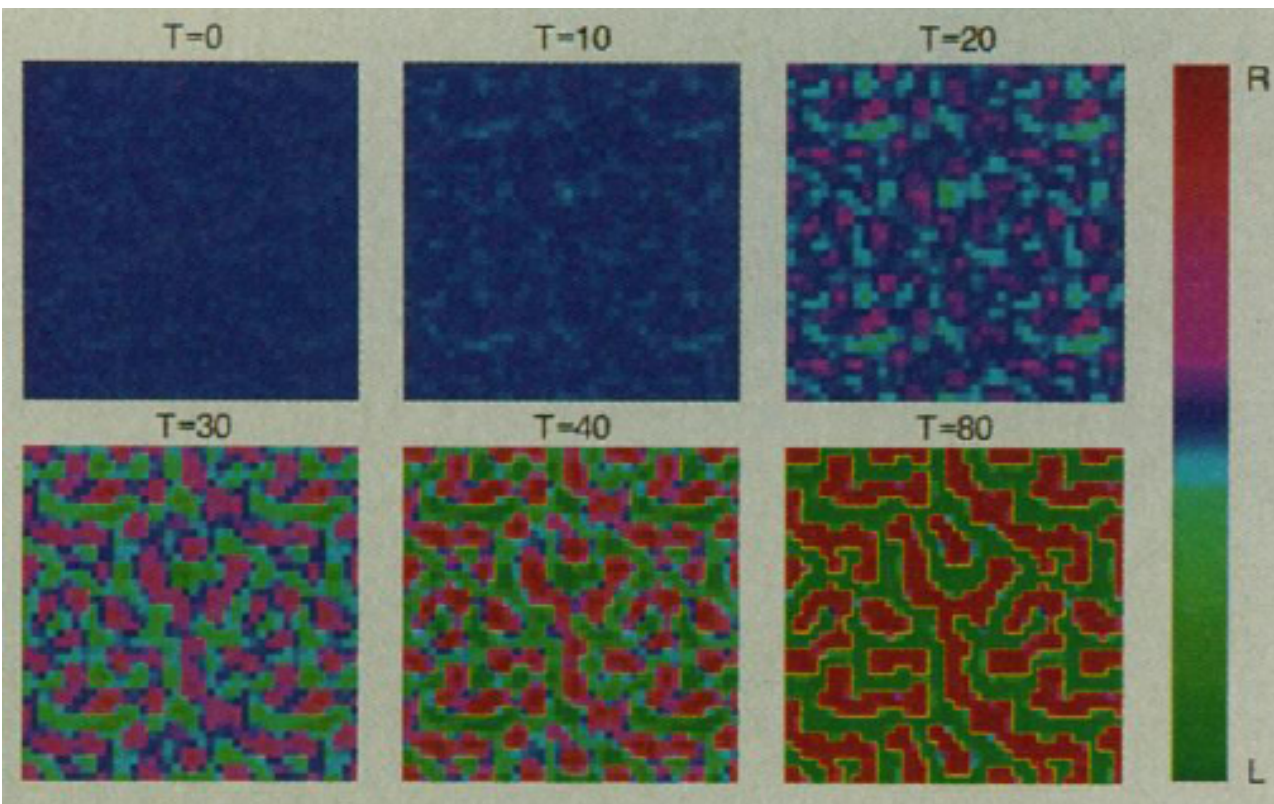


$$I(x - y)$$

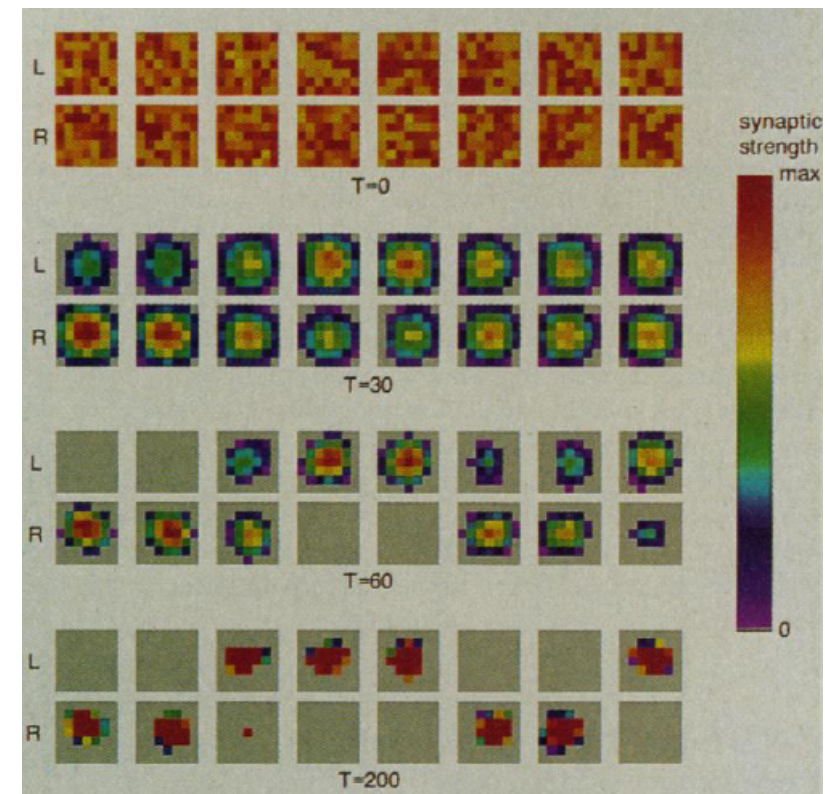


Results

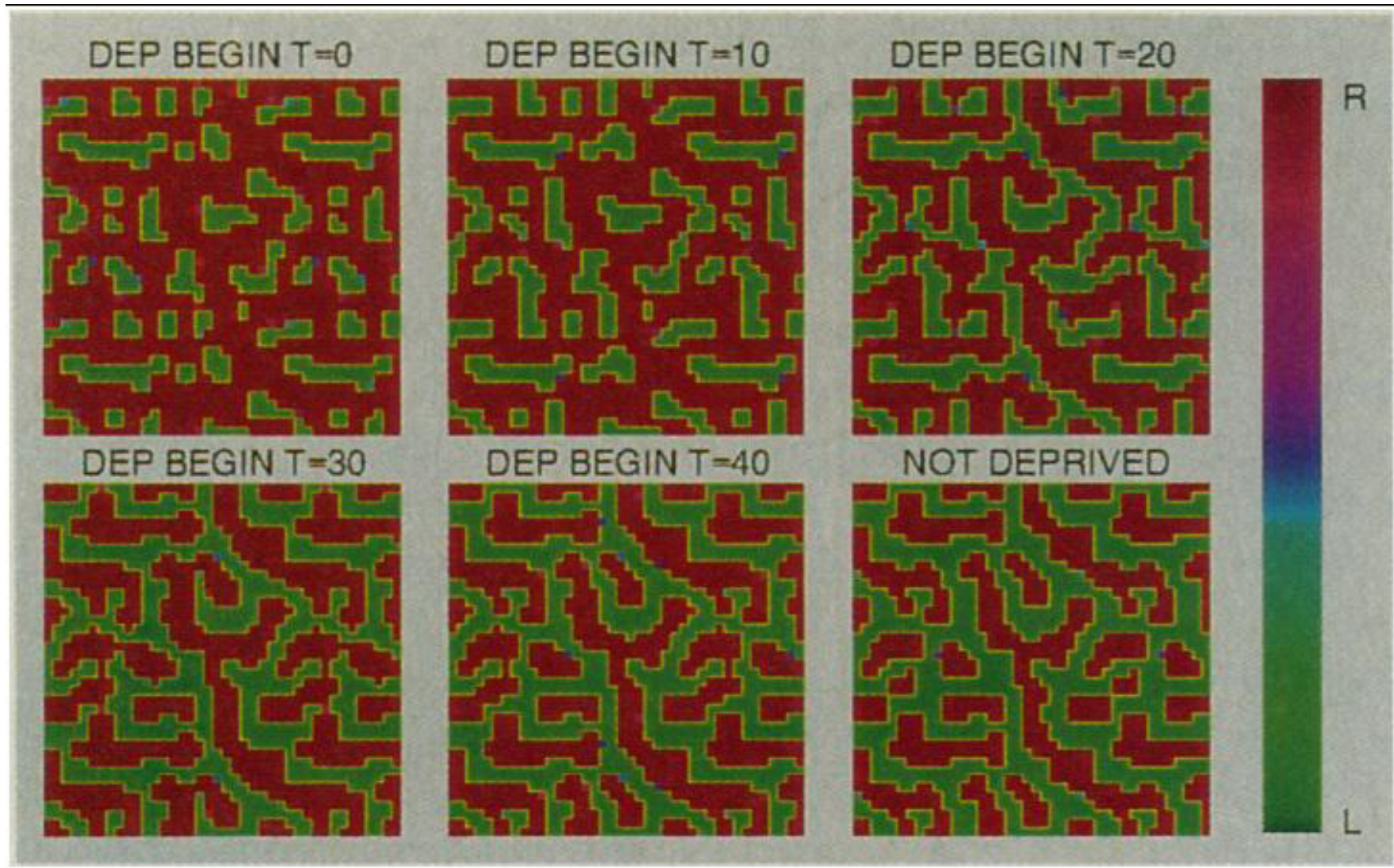
cortical map



receptive fields

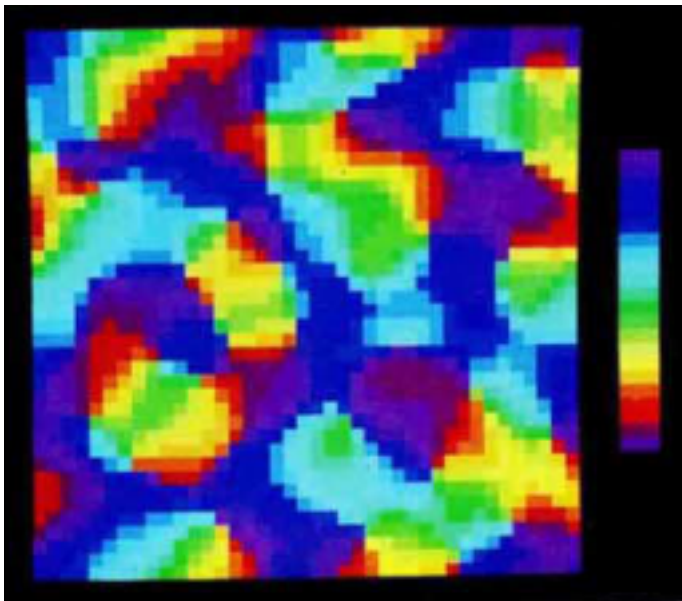


Simulation of monocular deprivation

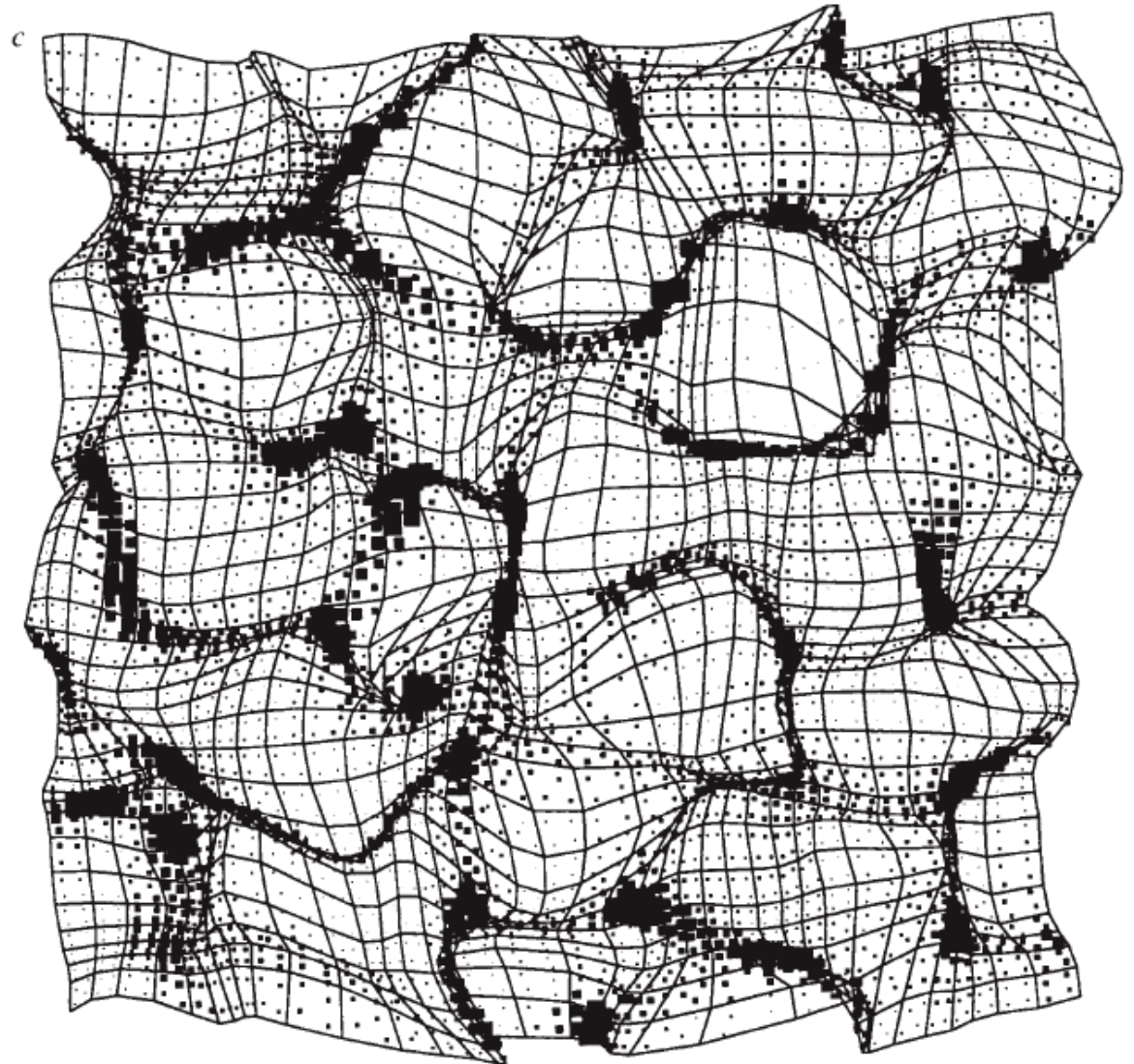


Elastic net model of position and orientation map (Durbin & Mitchison, 1990)

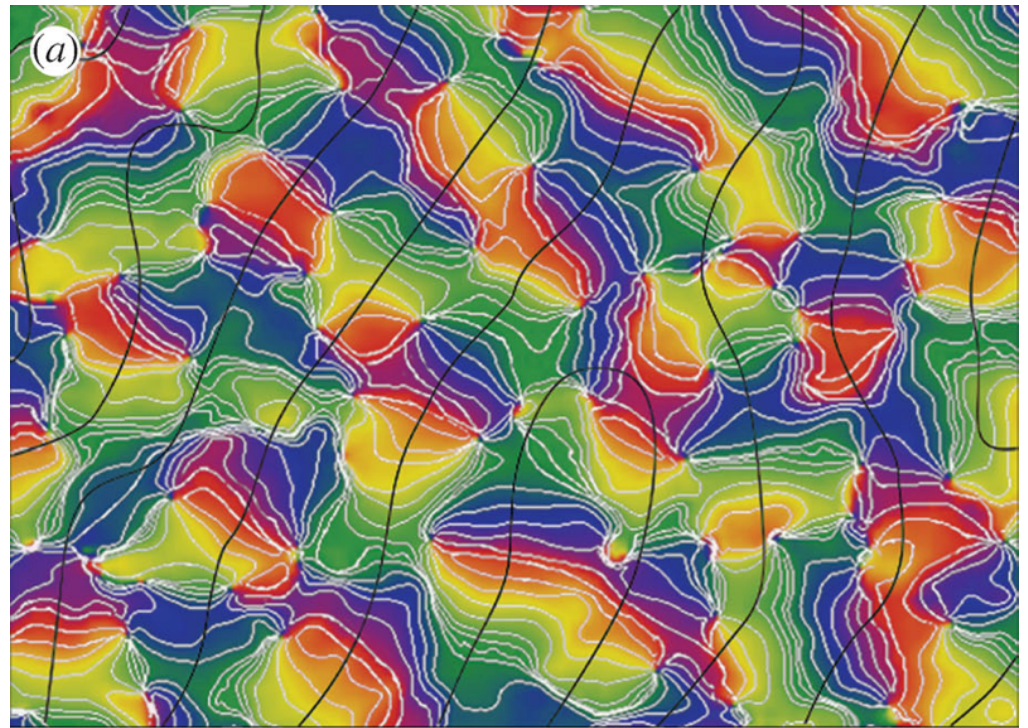
orientation map



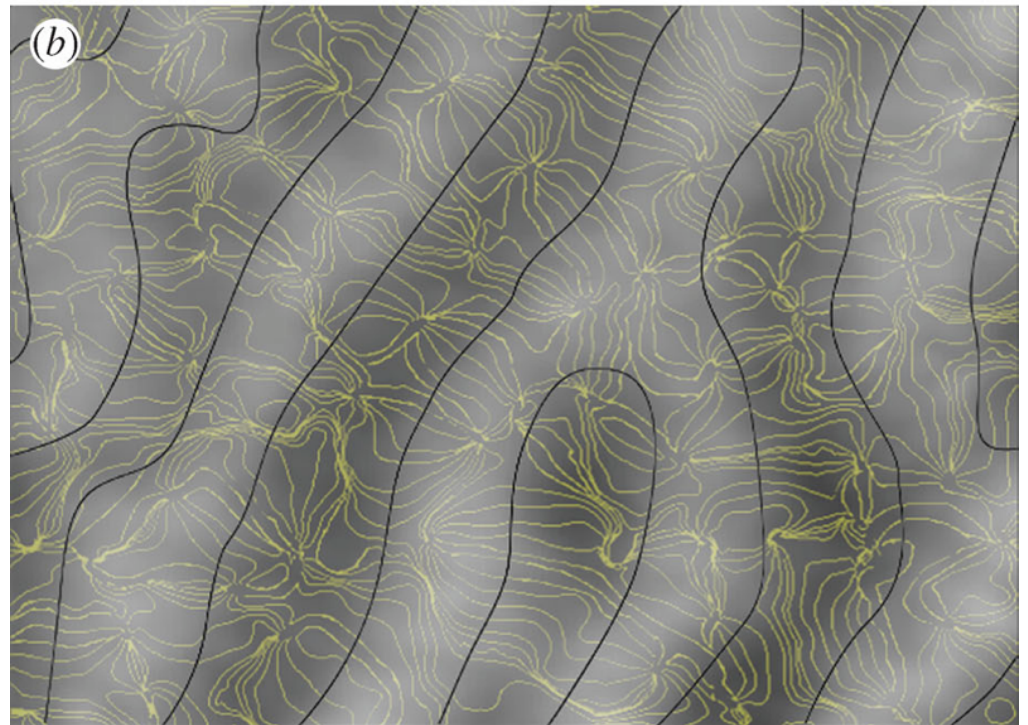
position map



Joint map of orientation and ocular dominance demonstrates tradeoff between feature diversity vs. smoothness within each feature dimension (from Blasdel 1992)



orientation columns



ocular dominance

The cortical column: a structure without a function

Jonathan C. Horton* and Daniel L. Adams

Beckman Vision Center, 10 Koret Way, University of California, San Francisco, CA 94143-0730, USA

This year, the field of neuroscience celebrates the 50th anniversary of Mountcastle's discovery of the cortical column. In this review, we summarize half a century of research and come to the disappointing realization that the column may have no function. Originally, it was described as a discrete structure, spanning the layers of the somatosensory cortex, which contains cells responsive to only a single modality, such as deep joint receptors or cutaneous receptors. Subsequently, examples of columns have been uncovered in numerous cortical areas, expanding the original concept to embrace a variety of different structures and principles. A 'column' now refers to cells in any vertical cluster that share the same tuning for any given receptive field attribute. In striate cortex, for example, cells with the same eye preference are grouped into ocular dominance columns. Unaccountably, ocular dominance

Although the column is an attractive concept, it has failed as a unifying principle for understanding cortical function. *Unravelling the organization of the cerebral cortex will require a painstaking description of the circuits, projections and response properties peculiar to cells in each of its various areas.*