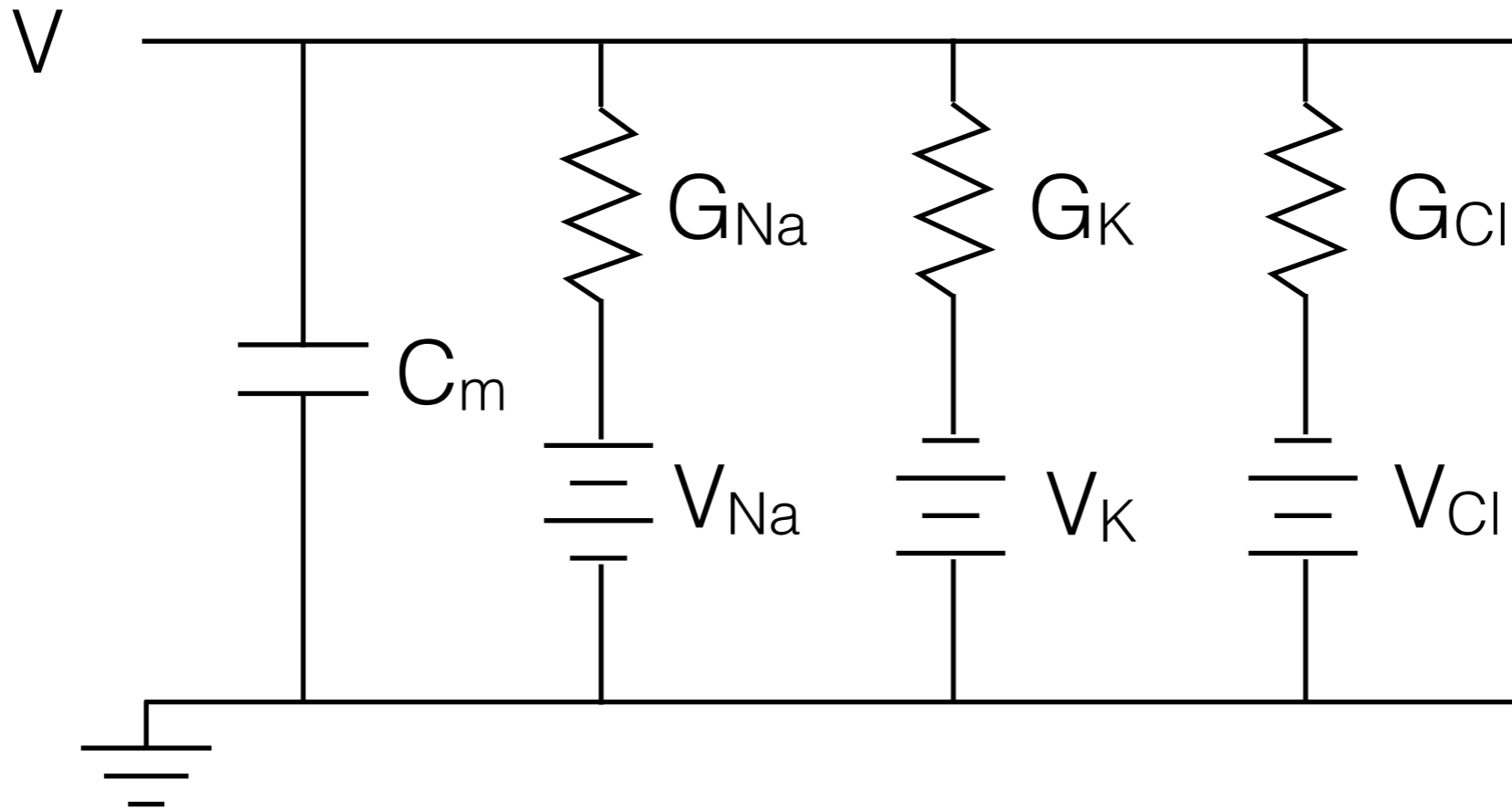


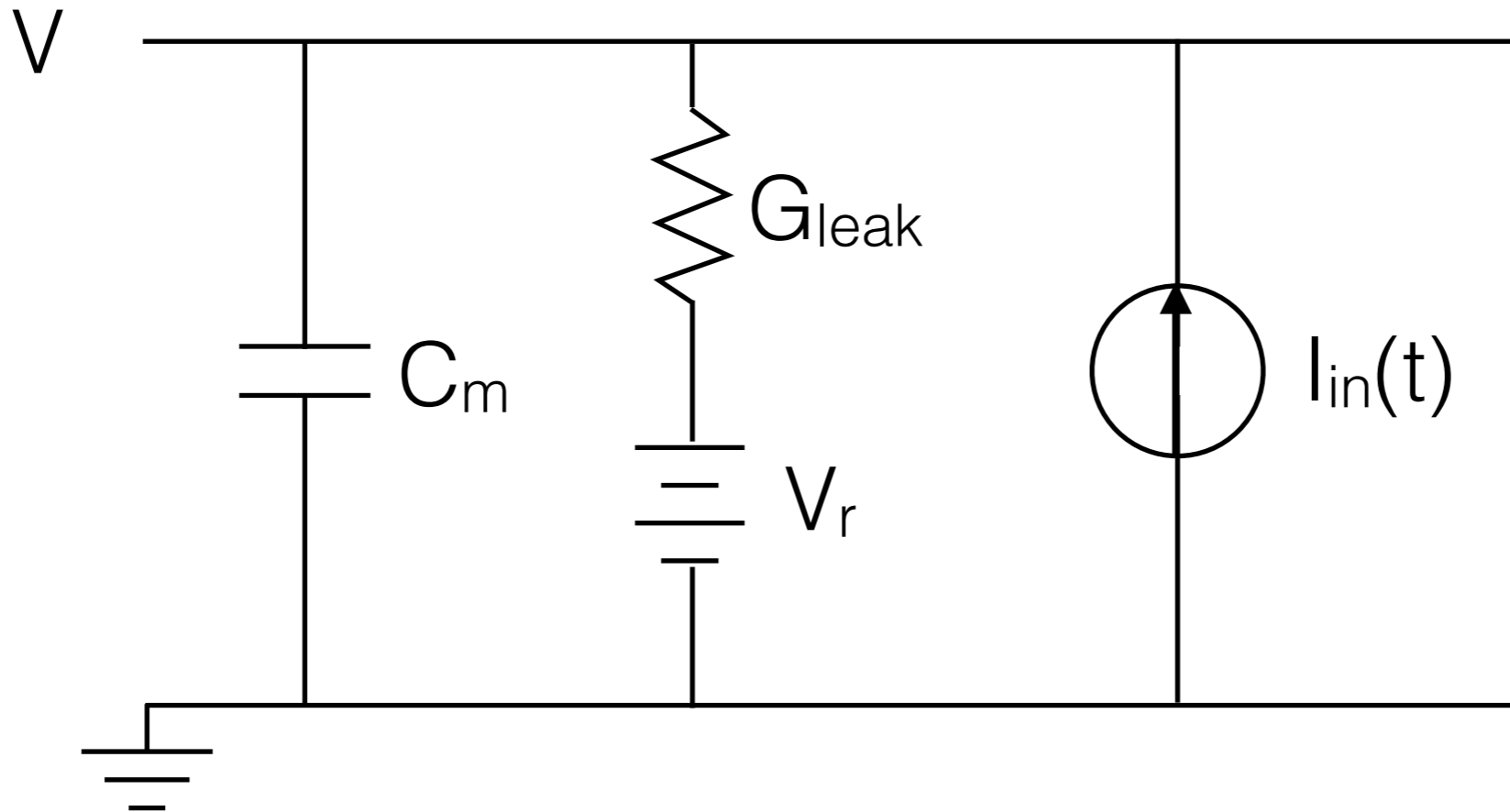
Membrane equation



$$\tau \frac{dV}{dt} + V = \frac{V_{Na} G_{Na} + V_K G_K + V_{Cl} G_{Cl}}{G_{total}}$$

$$G_{total} = G_{Na} + G_K + G_{Cl} \quad \tau = \frac{C_m}{G_{total}}$$

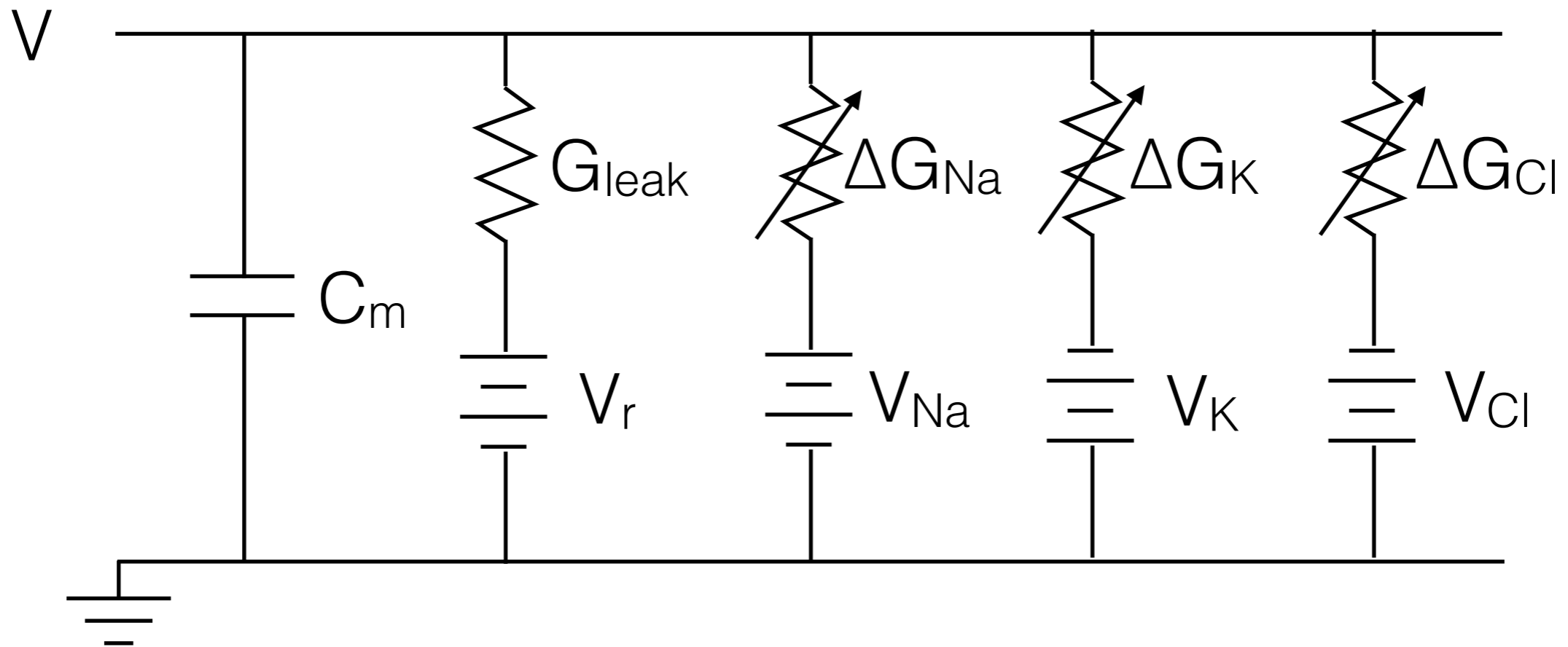
Membrane with input current



$$\tau \frac{dV}{dt} + V = V_r + \frac{1}{G_{\text{leak}}} I_{\text{in}}(t)$$

$$G_{\text{leak}} = G_{Na} + G_K + G_{Cl} \quad \tau = \frac{C_m}{G_{\text{leak}}}$$

Membrane with synaptic inputs



$$\tau \frac{dV}{dt} + V = \frac{V_r G_{\text{leak}} + V_{\text{Na}} \Delta G_{\text{Na}} + V_{\text{K}} \Delta G_{\text{K}} + V_{\text{Cl}} \Delta G_{\text{Cl}}}{G_{\text{total}}}$$

$$G_{\text{total}} = G_{\text{leak}} + \Delta G_{\text{Na}} + \Delta G_{\text{K}} + \Delta G_{\text{Cl}} \quad \tau = \frac{C_m}{G_{\text{total}}}$$

Channel types

Passive

$$G_{\text{ion}} = f(\text{molecules_outside})$$

ionotropic

$$G_{\text{ion}} = f(\text{molecules_inside})$$

$$\text{molecules_inside} = g(\text{molecules_outside})$$

metabotropic

$$G_{\text{ion}} = f(\text{light_intensity})$$

photoreceptor

$$G_{\text{ion}} = f(\text{mechanical_deflection})$$

hair cell

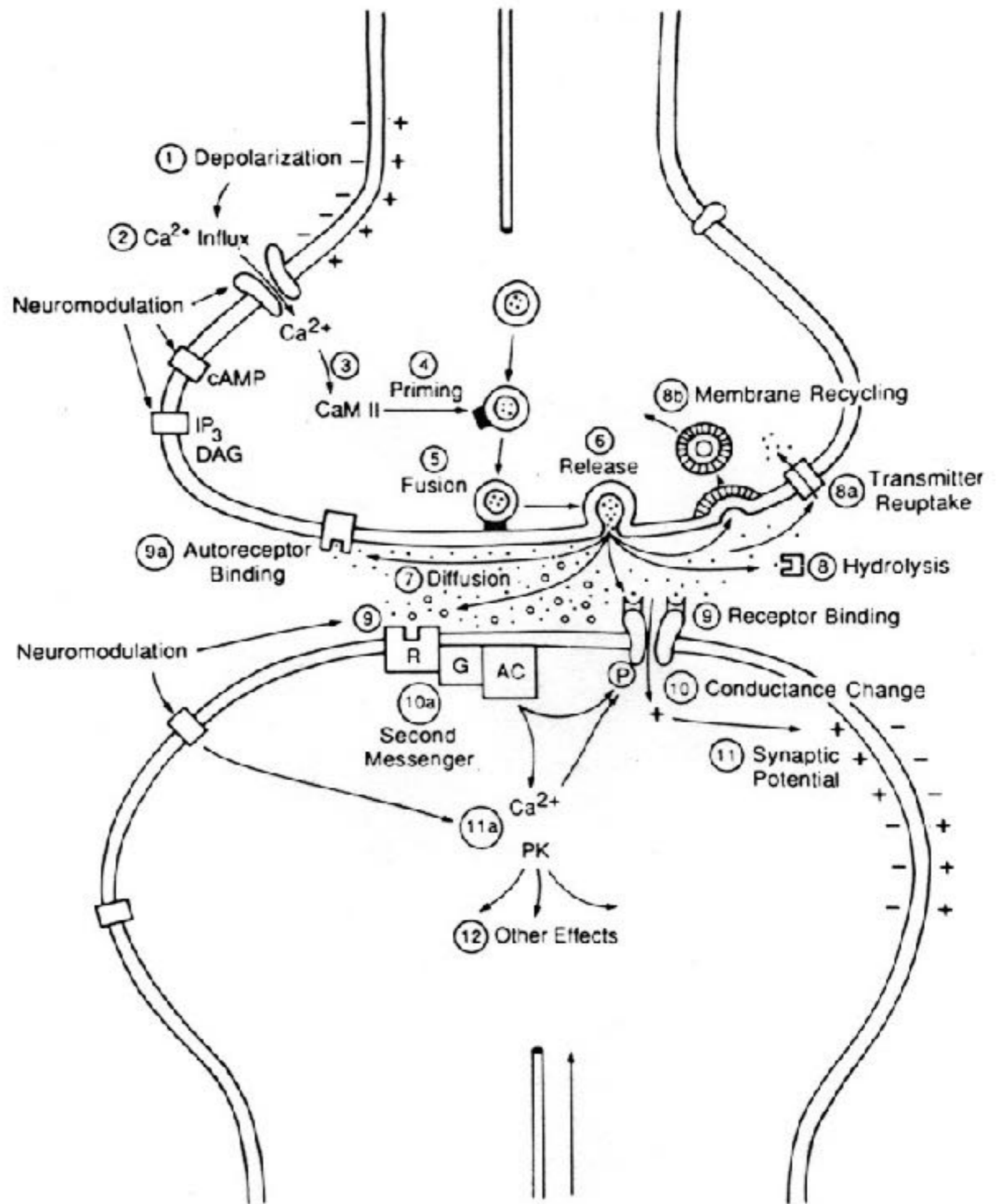
‘Active’*

$$G_{\text{ion}} = f(\text{membrane_voltage})$$

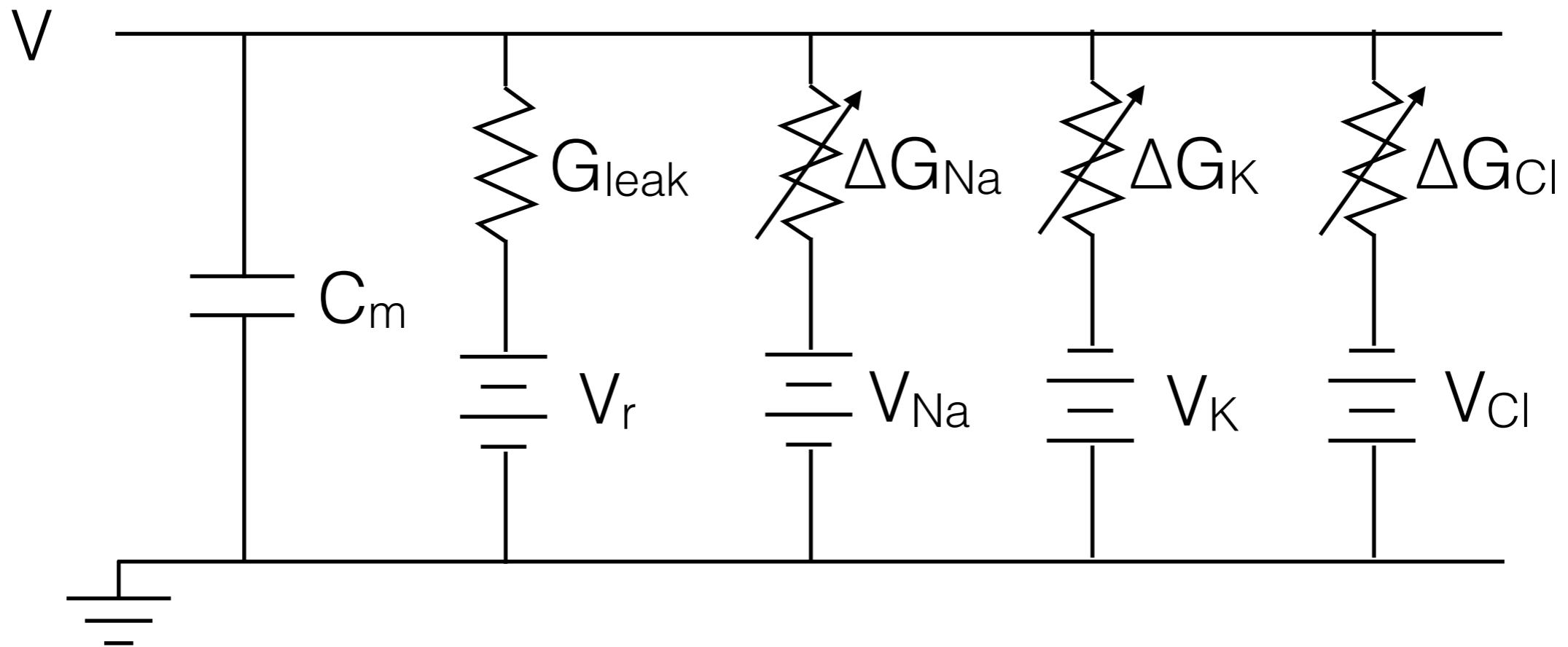
voltage-gated

*in the sense of providing gain, not in the sense of requiring active ATP transport

Anatomy of a synapse

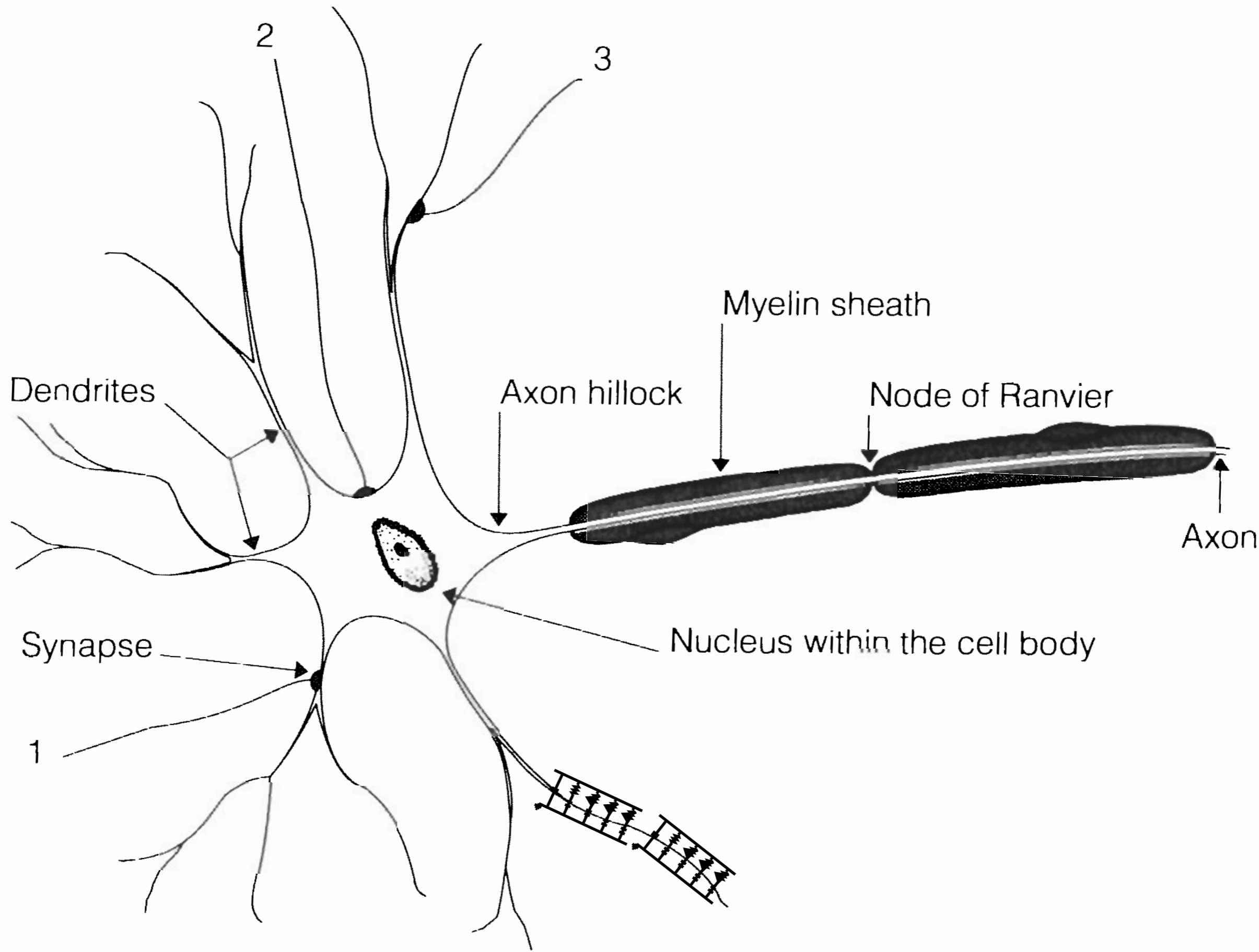


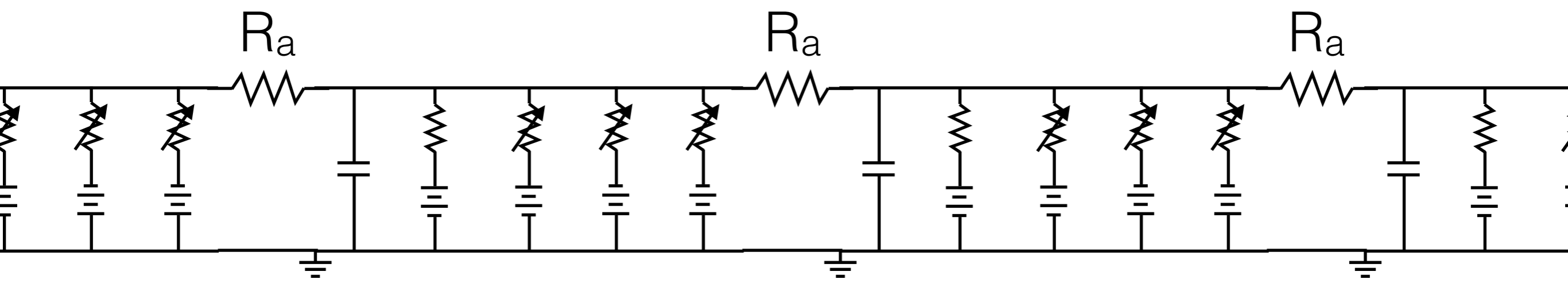
Membrane with synaptic inputs



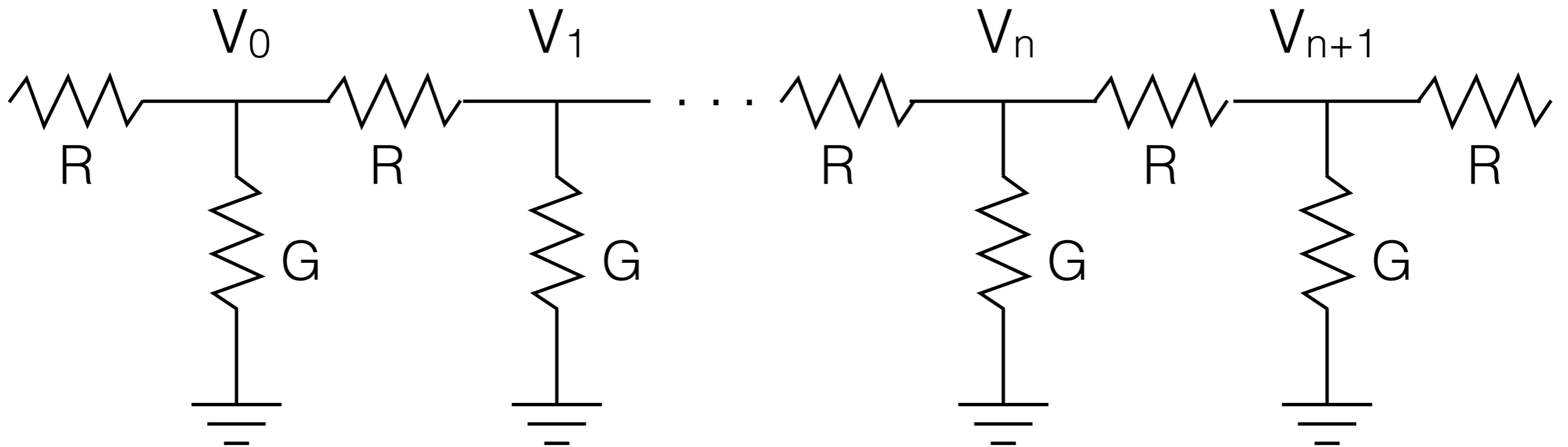
$$\tau \frac{dV}{dt} + V = \frac{V_r G_{\text{leak}} + V_{\text{Na}} \Delta G_{\text{Na}} + V_{\text{K}} \Delta G_{\text{K}} + V_{\text{Cl}} \Delta G_{\text{Cl}}}{G_{\text{total}}}$$

$$G_{\text{total}} = G_{\text{leak}} + \Delta G_{\text{Na}} + \Delta G_{\text{K}} + \Delta G_{\text{Cl}} \quad \tau = \frac{C_m}{G_{\text{total}}}$$





Resistive network



$$\frac{d^2 V}{dx^2} = R G V$$

$$V = V_0 e^{-\frac{|x|}{L}}$$

$$L = 1/\sqrt{R G}$$